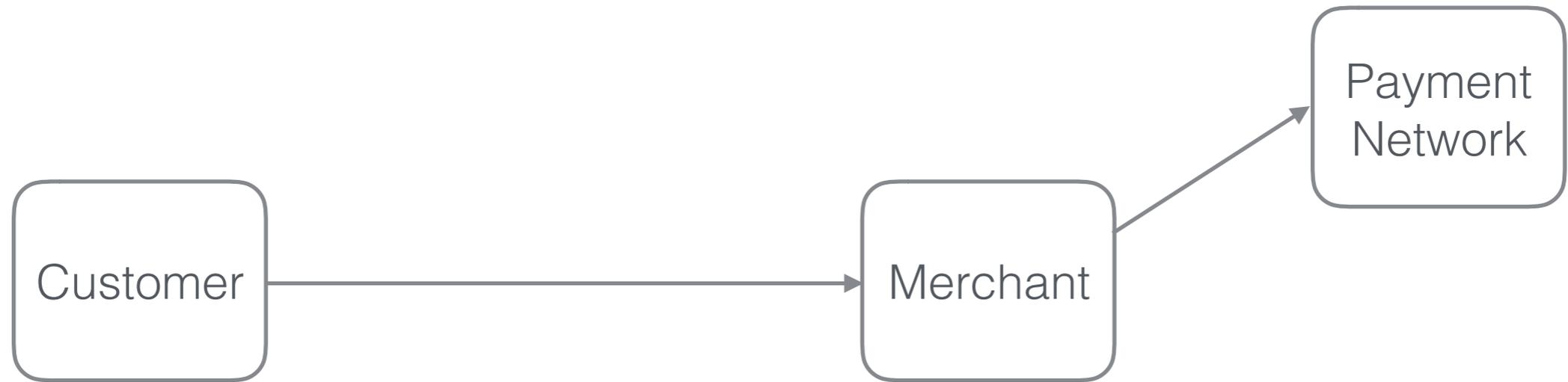


# Decentralized Anonymous Micropayments

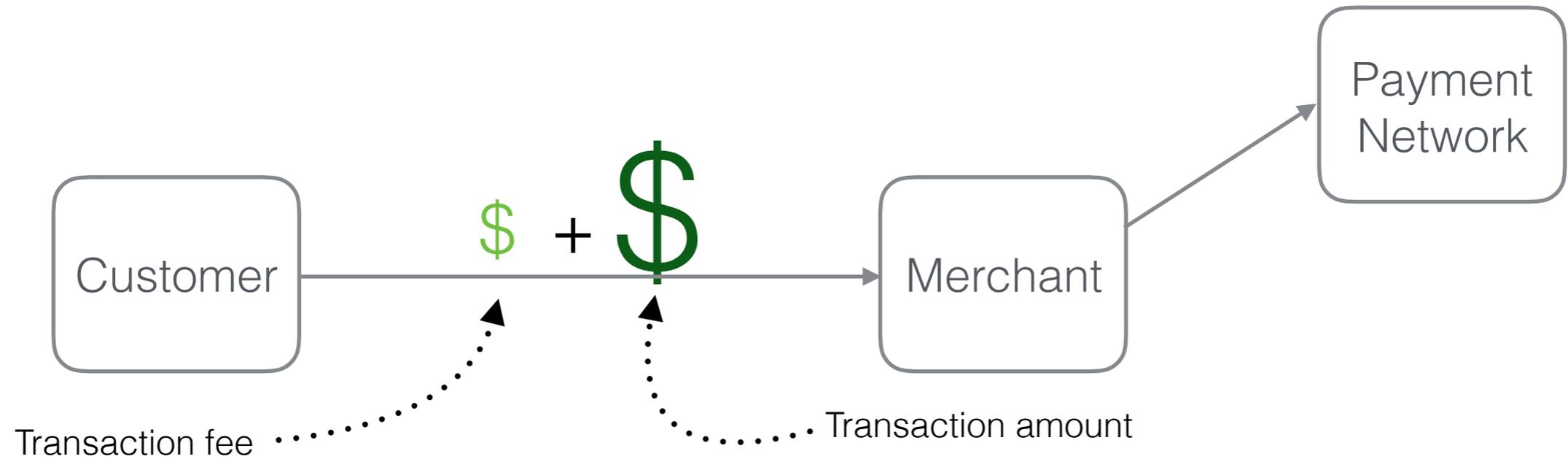
Alessandro Chiesa, Matthew Green, Jingcheng Liu,  
Peihan Miao, Ian Miers, **Pratyush Mishra**

<http://eprint.iacr.org/2016/1033>

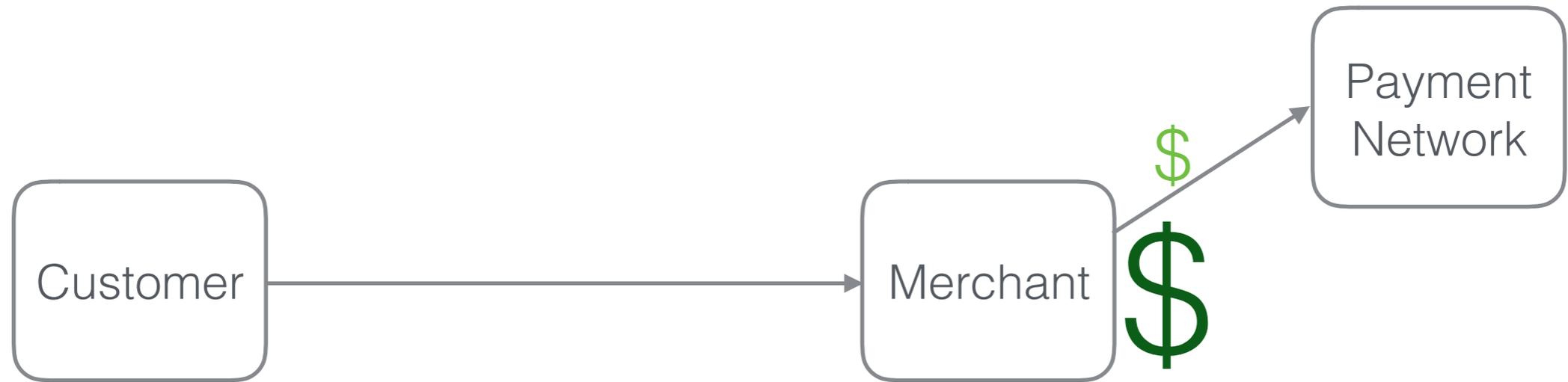
# Digital Payments



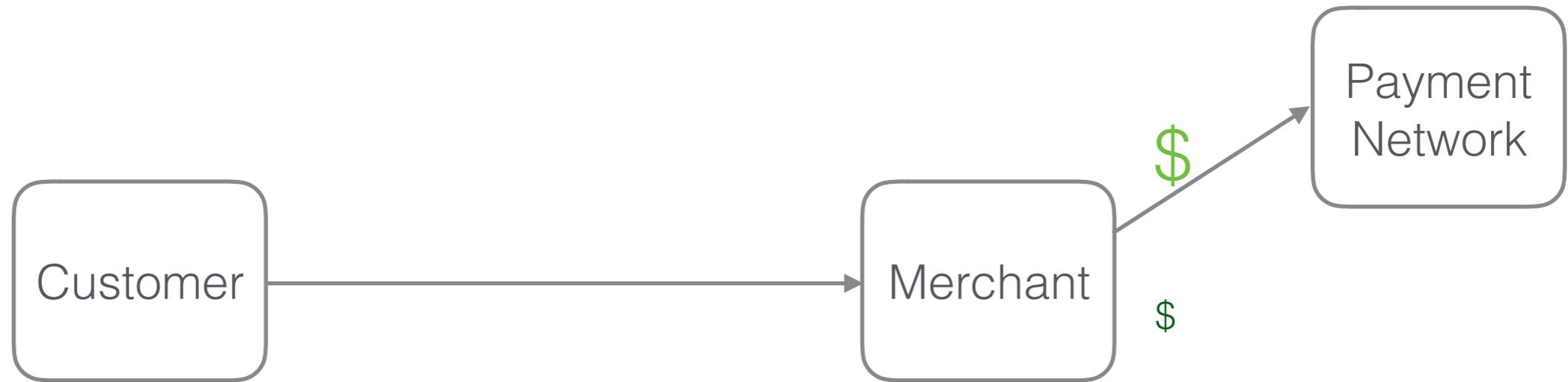
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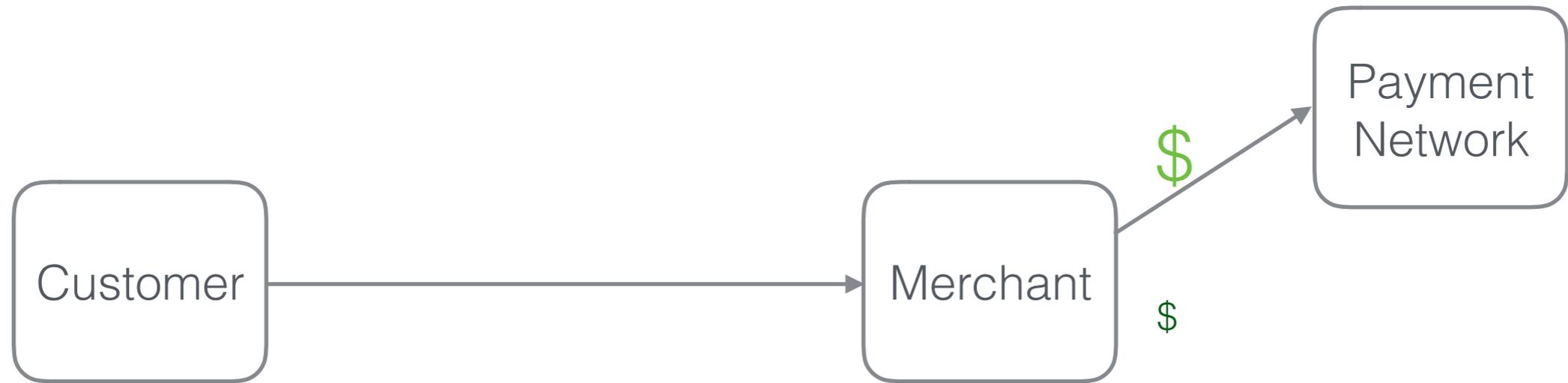
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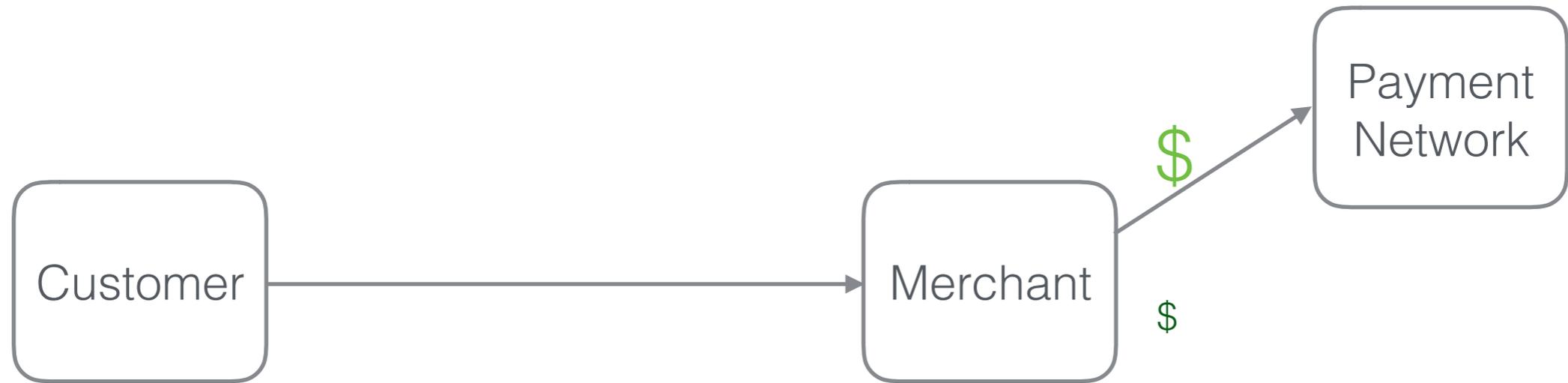


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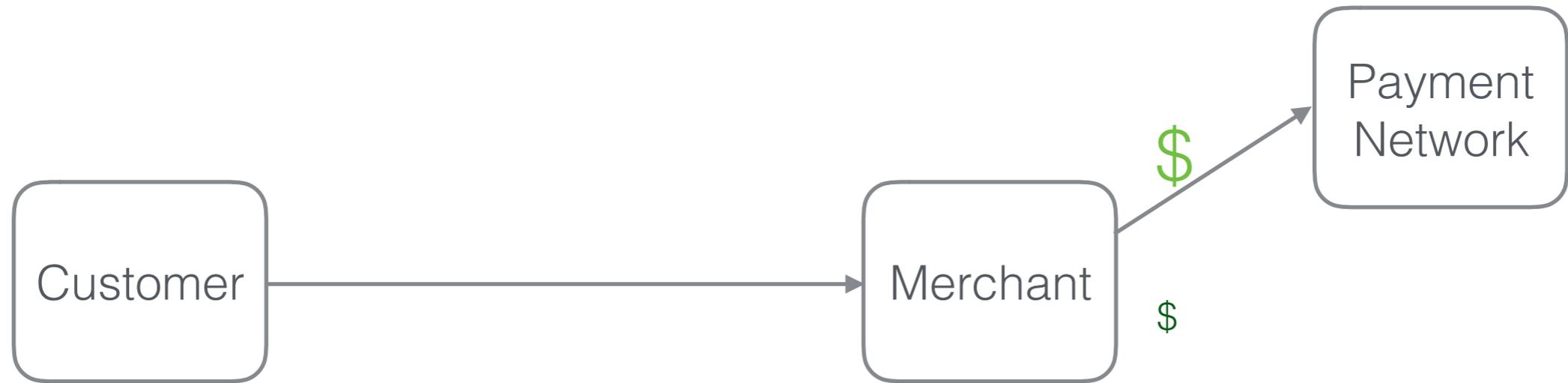
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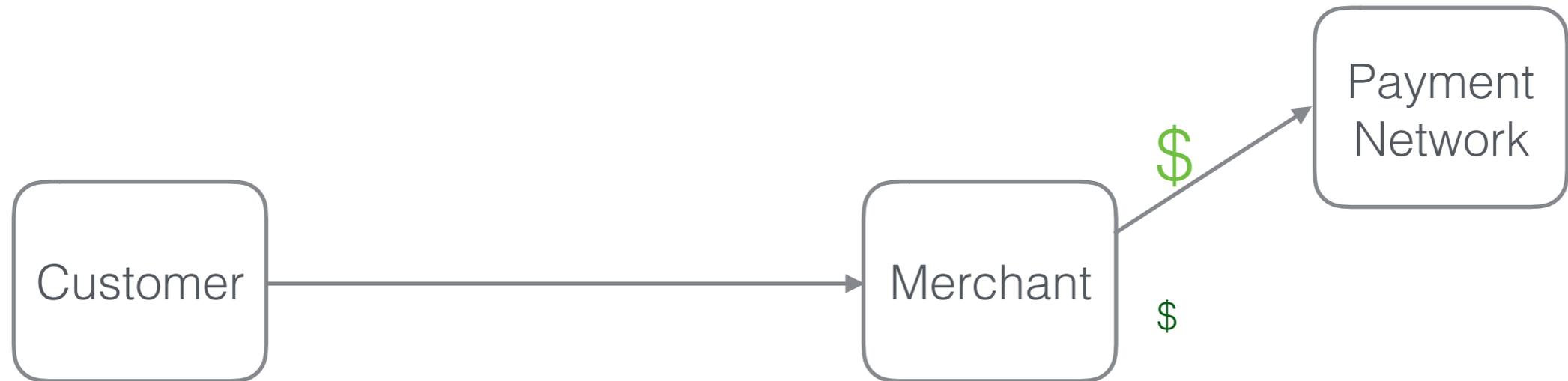


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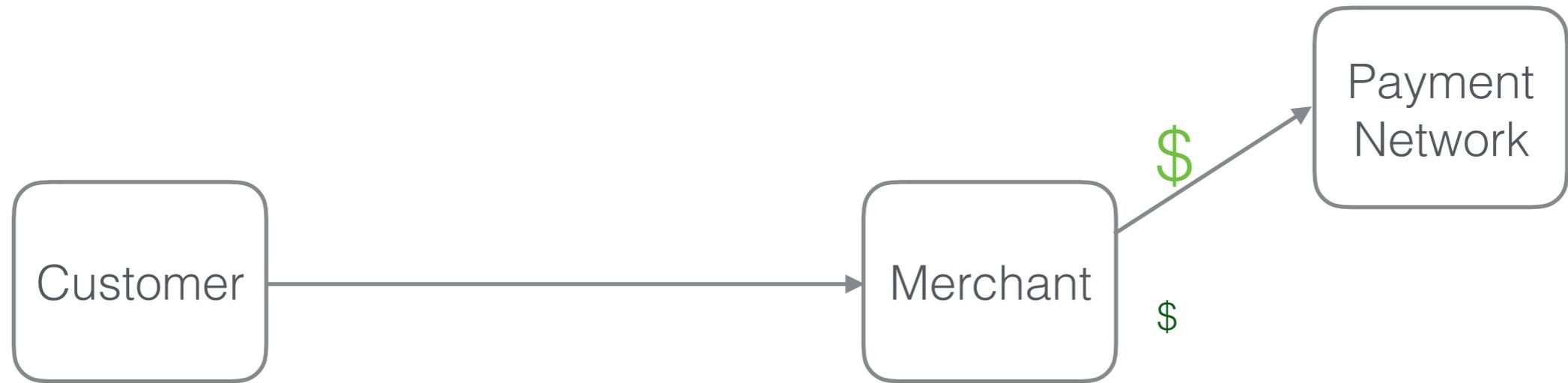
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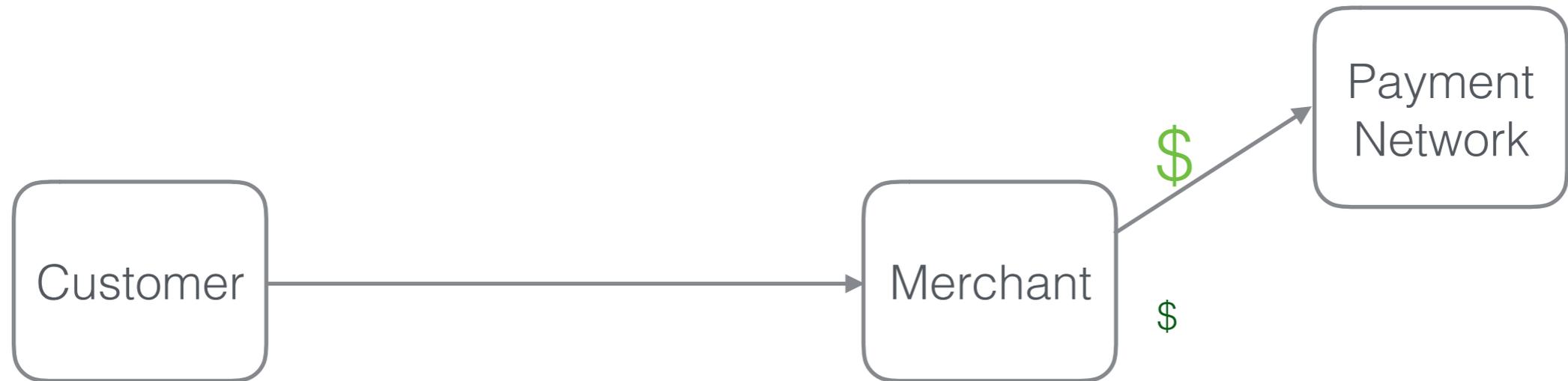
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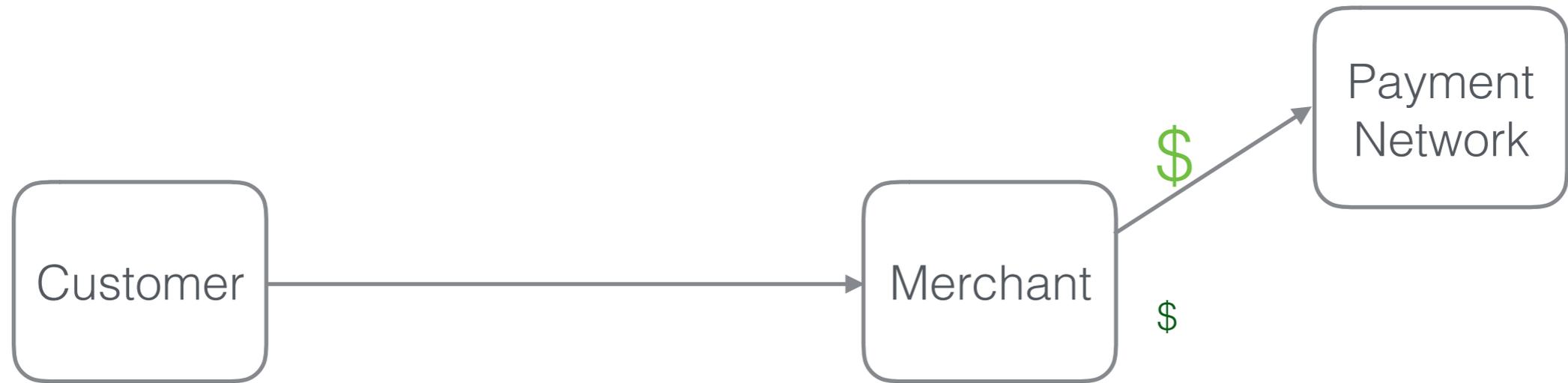
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... but no widespread deployments across multiple merchants.

Potential reason: Prior systems required central mediator.

Why? Requires creating financial relations, meeting regulations, etc.



# Bitcoin

- Decentralized currency w/ quick adoption.
- No need to establish business relations between banks, merchants and regulators.
- To pay, just sign “**from A to B: amt 4.3**”.



LEDGER			
From	To	Amt	Sign
	⋮		
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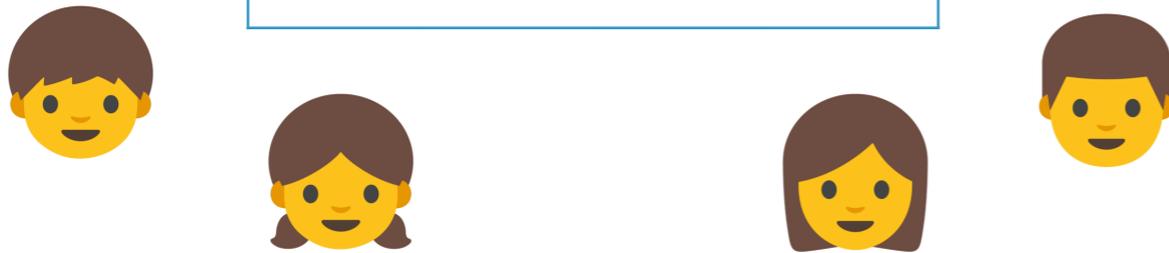
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- Probabilistic payments for Bitcoin.
- **Solves problem 1:** Amortized tx fee.
- **Solves problem 2:** Quick confirmation.

### Zerocash (Oakland 2014)

- Anonymous Bitcoin-like currency.
- **Solves problem 3:** Hides sender, receiver and amount.

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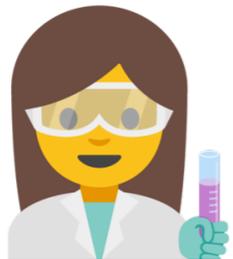
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(probabilistic)
  - **game theory**: characterization of double-spending.

# Probabilistic Payments

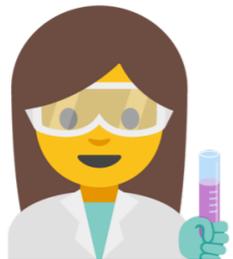
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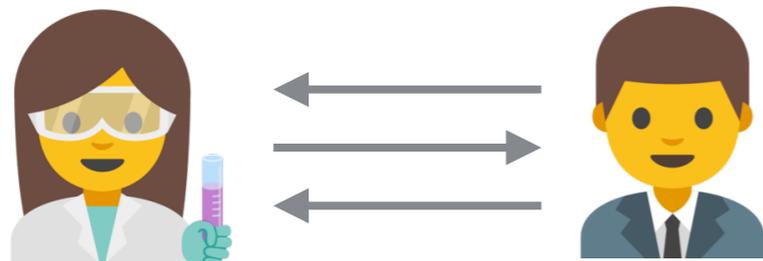


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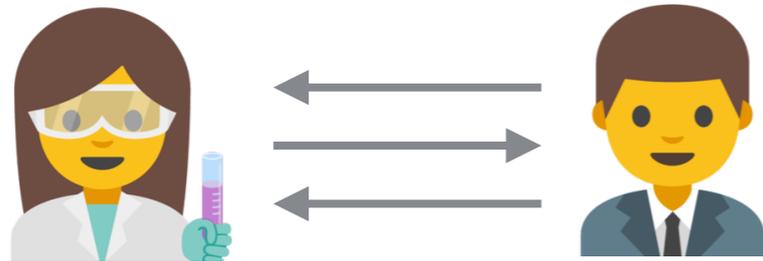
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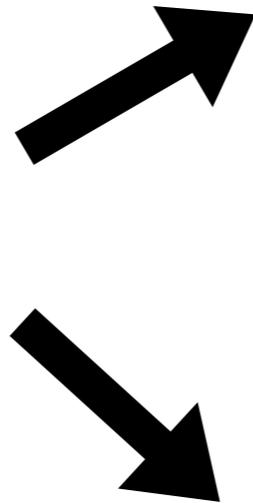
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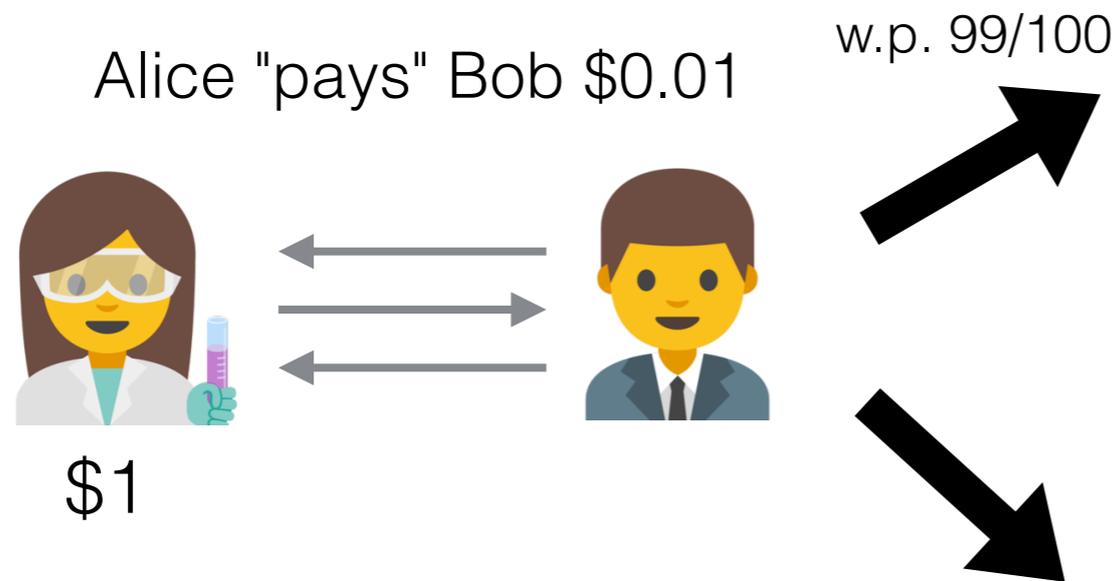
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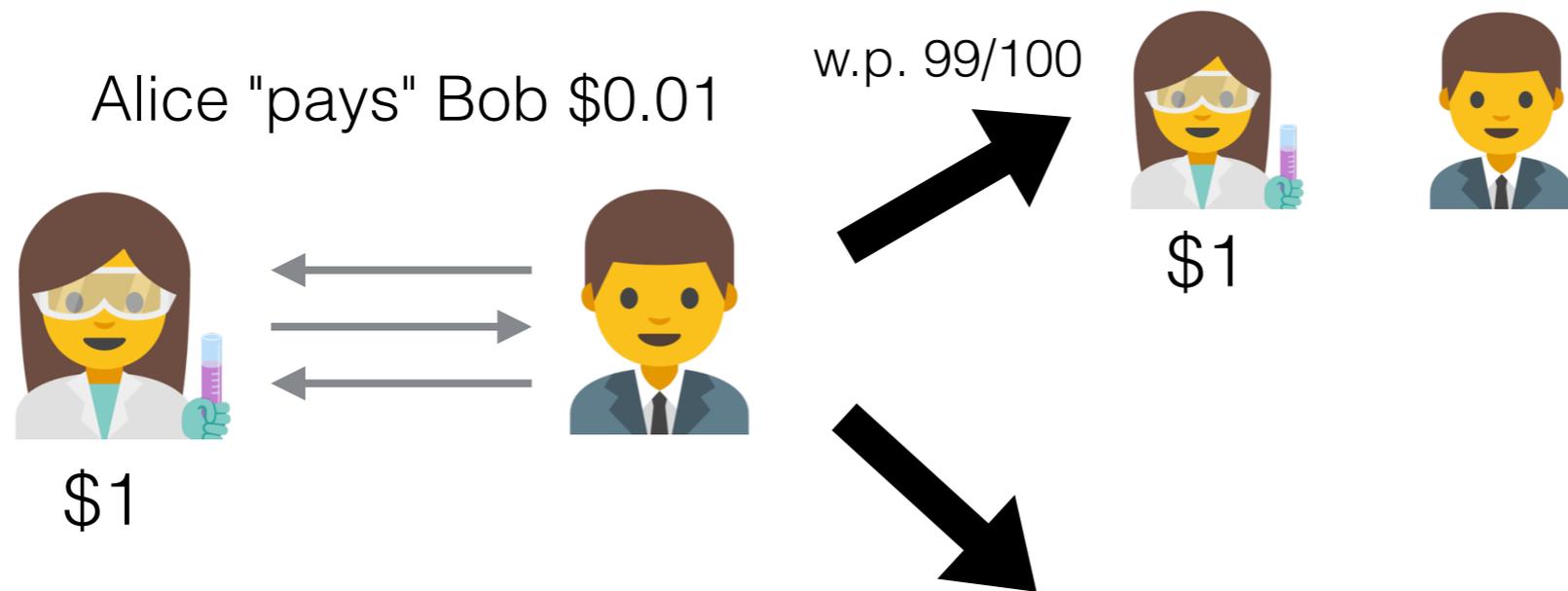
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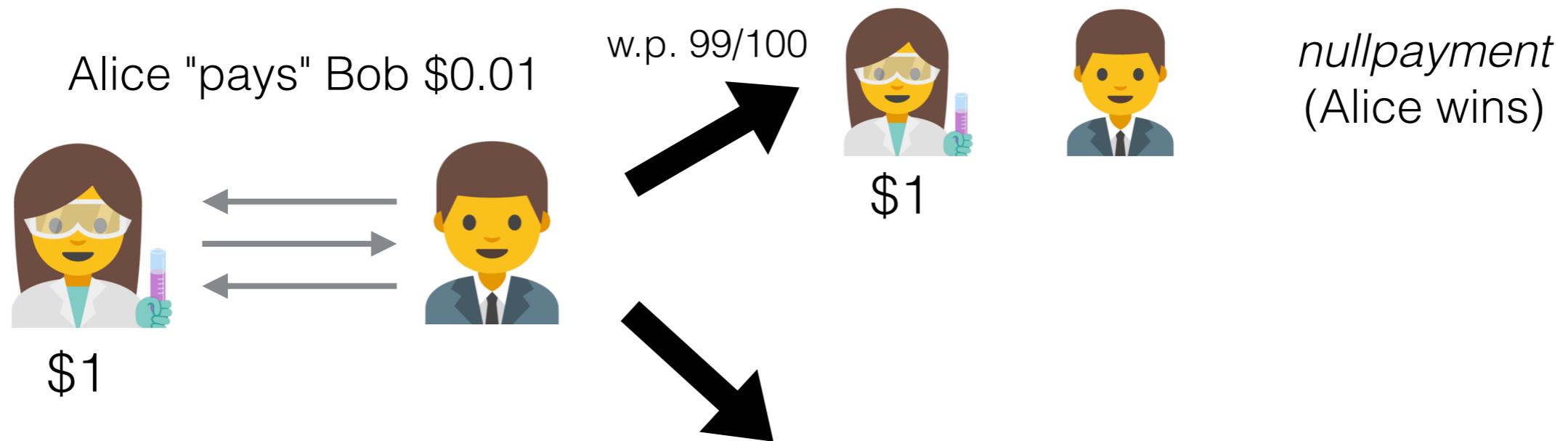
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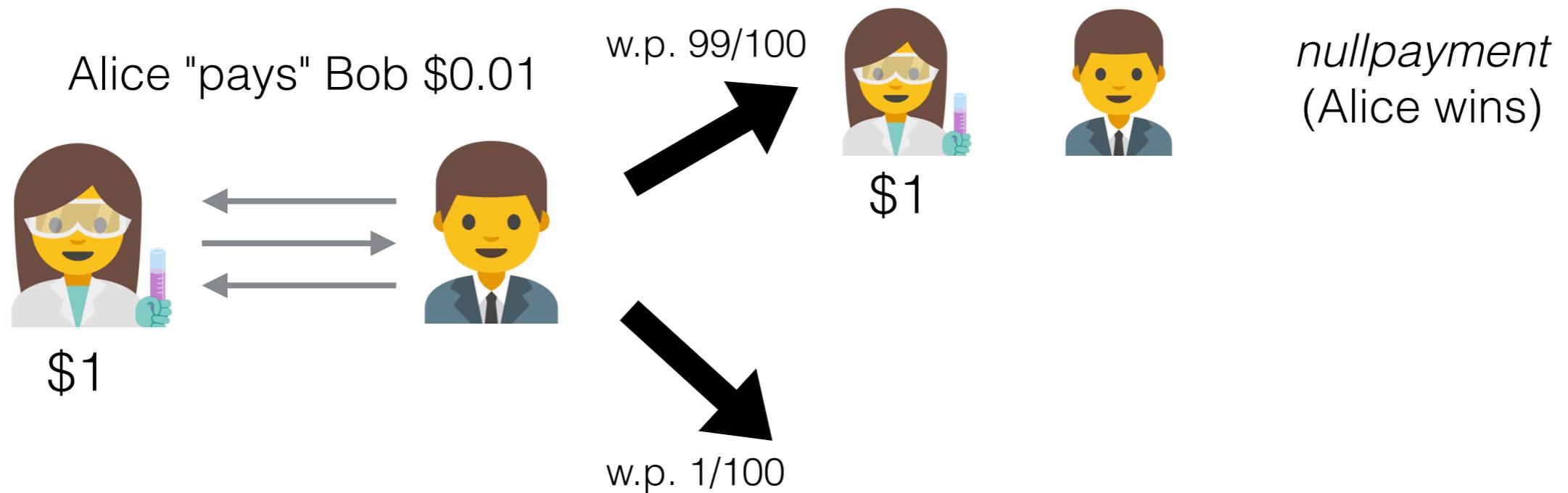
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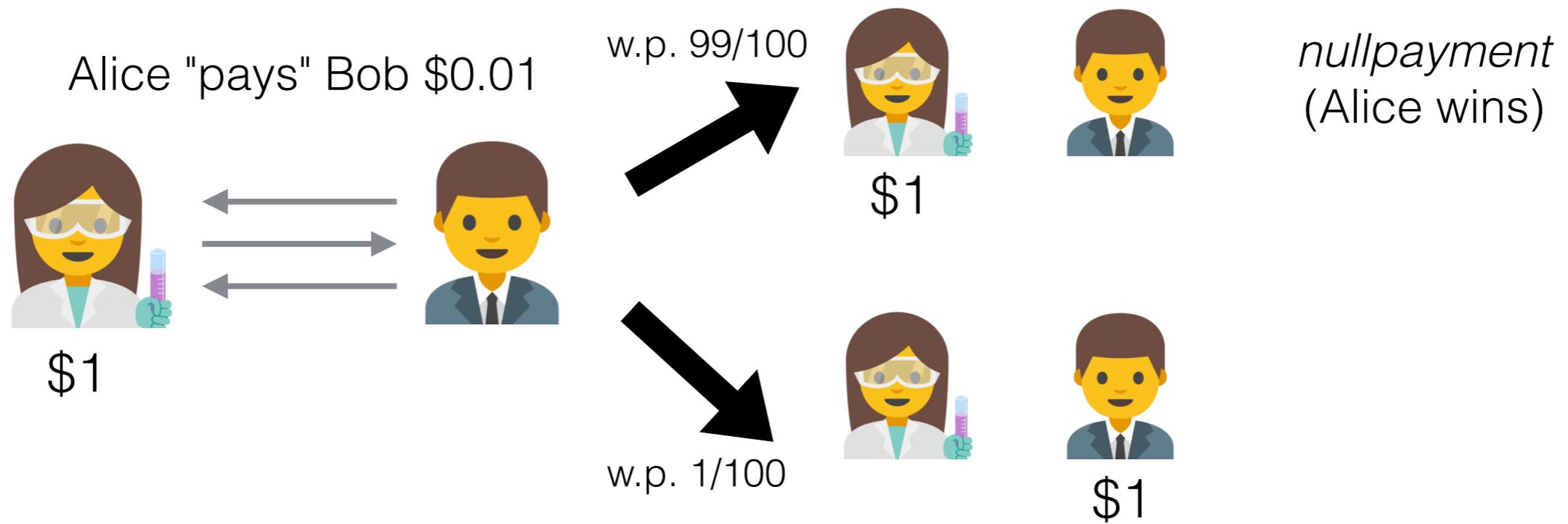
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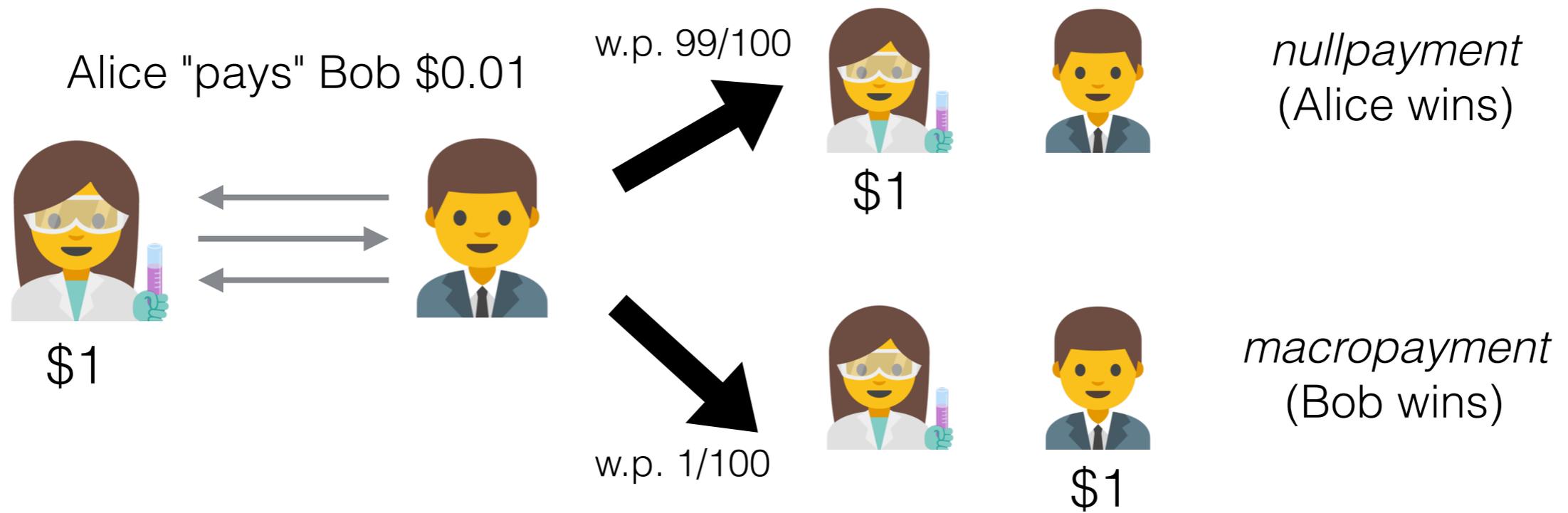
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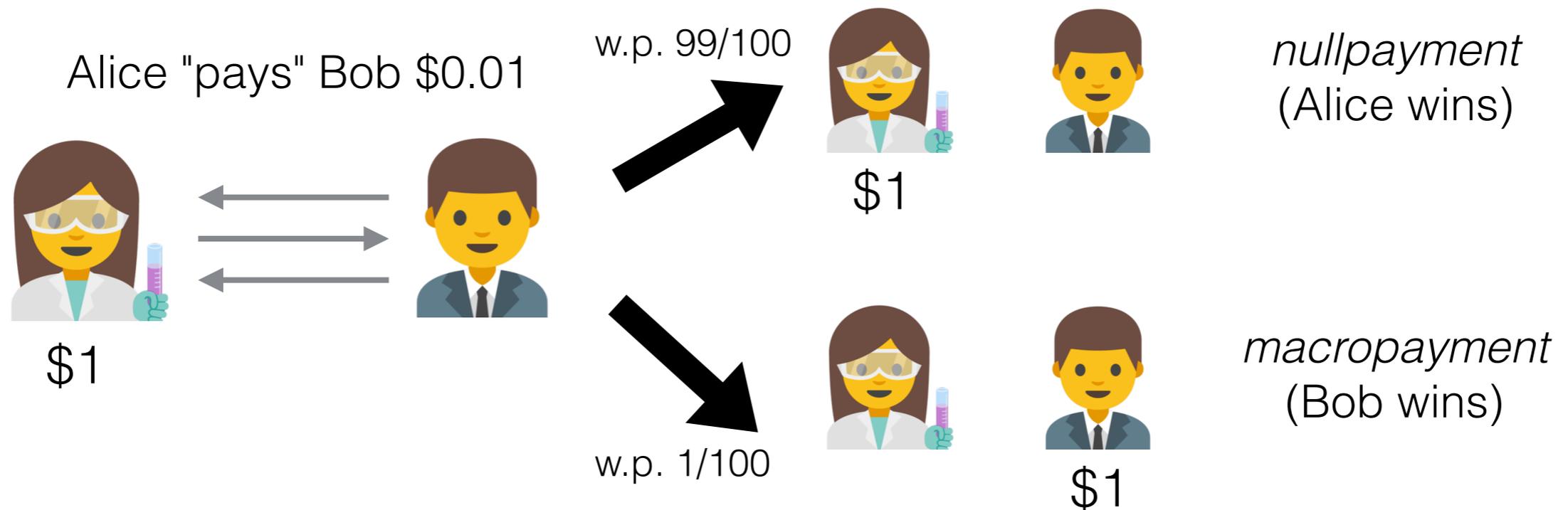
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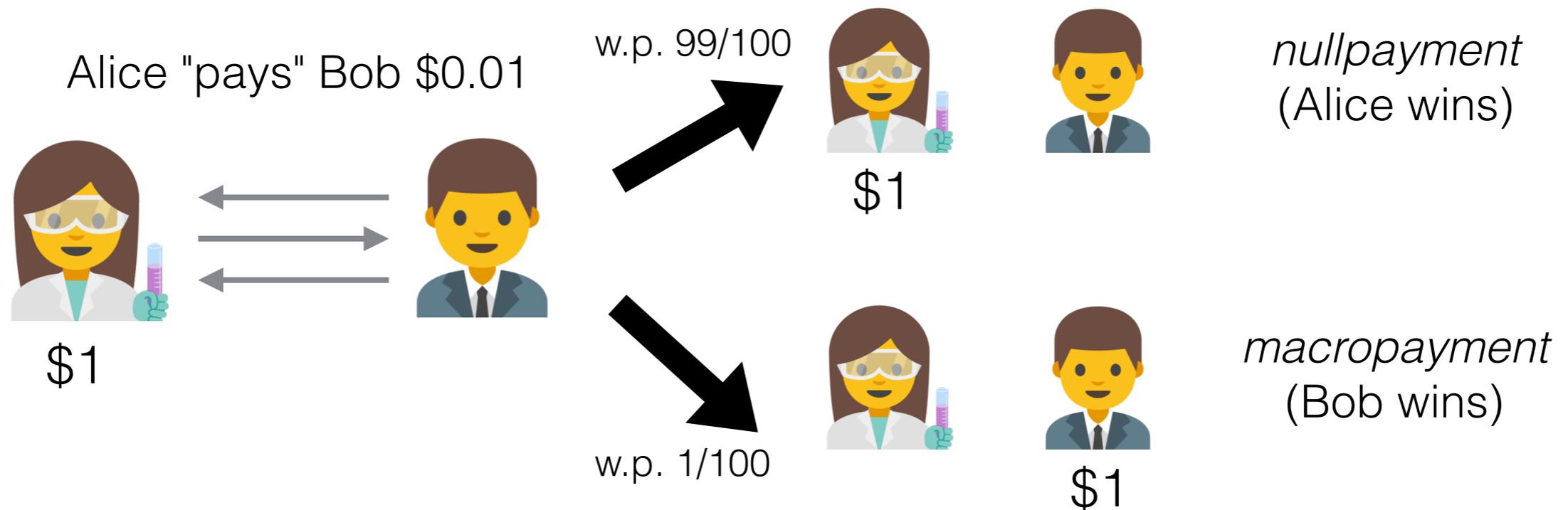


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**Probabilistic payments imply micropayments:**

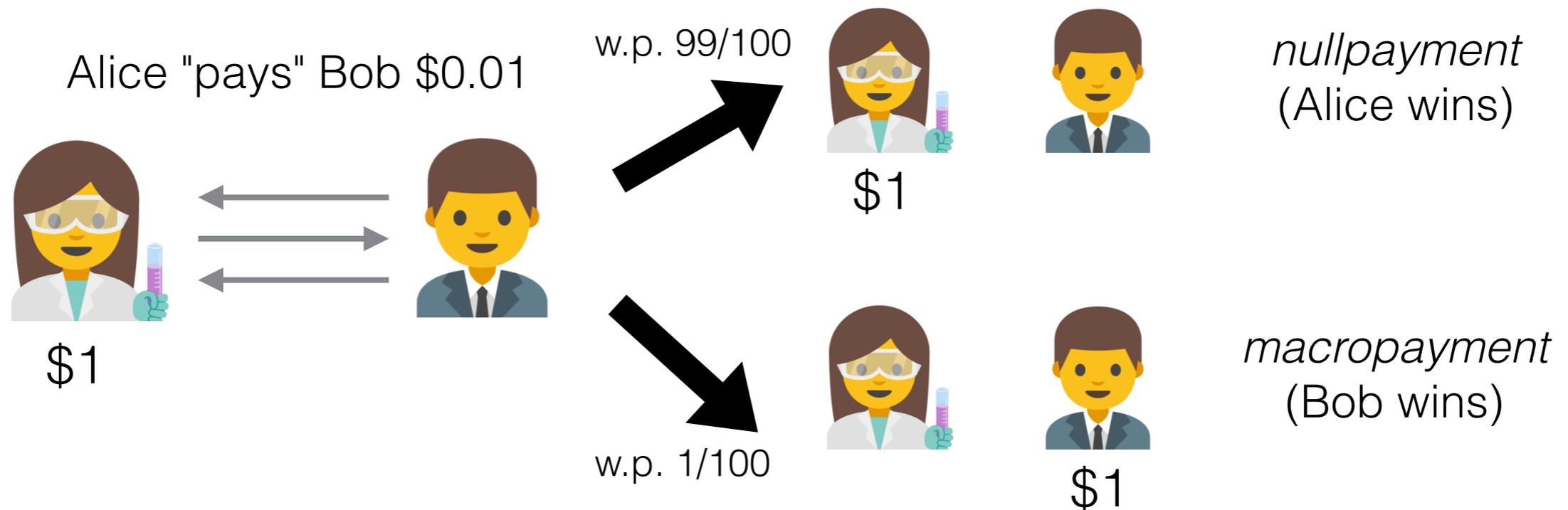
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## **Probabilistic payments imply micropayments:**

Transaction fee is amortized over many payments.

# Probabilistic Payments



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Nullpayments are offline and do not require interaction with payment network.

# Building Blocks

Pass-Shelat

Zerocash



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Pass-Shelat  
coin-flipping + Bitcoin

Zerocash

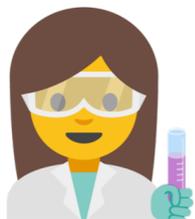


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A	M	10	$\sigma_A$



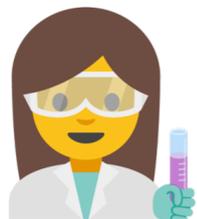
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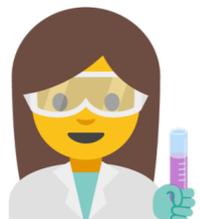
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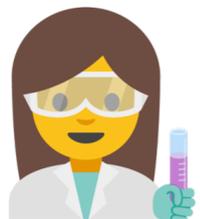
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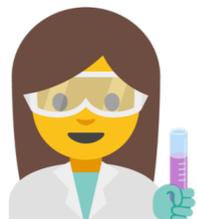
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E	B	4.3	$\sigma_E$



← coin-flip →



## Zerocash

zero knowledge proofs + Bitcoin

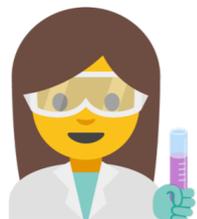
# Building Blocks

## Pass-Shelat

coin-flipping + Bitcoin

1. Alice escrows  $v$ .
2. Alice and Bob engage in coin-flip.
3. If Alice wins: she can reuse escrow.
4. If Bob wins: he gets  $v$ .

Ledger			
From	To	Amt	Sign
		⋮	
M	N	2.3	$\sigma_M$
A	M	10	$\sigma_A$
A	E	4.3	$\sigma_A$
E	B	4.3	$\sigma_E$



← coin-flip →



## Zerocash

zero knowledge proofs + Bitcoin

Ledger		
Old	New	Proof
		⋮
8436378	$cm_1$	$\pi_1$
6327690	$cm_2$	$\pi_2$

$pk_A, sk_A$



$pk_B, sk_B$



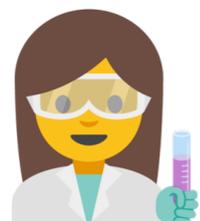
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coin-flipping + Bitcoin

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From	To	Amt	Sign
		⋮	
M	N	2.3	$\sigma_M$
A	M	10	$\sigma_A$
A	E	4.3	$\sigma_A$
E	B	4.3	$\sigma_E$



← coin-flip →



## Zerocash

zero knowledge proofs + Bitcoin

1. Alice owns coin  $c_1$  with comm  $cm_1$ .



$pk_A, sk_A$



Ledger		
Old	New	Proof
		⋮
8436378	$cm_1$	$\pi_1$
6327690	$cm_2$	$\pi_2$

$pk_B, sk_B$



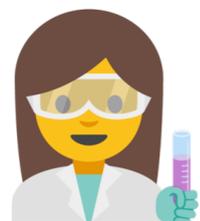
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coin-flipping + Bitcoin

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3. If Alice wins: she can reuse escrow.
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Ledger			
From	To	Amt	Sign
		⋮	
M	N	2.3	$\sigma_M$
A	M	10	$\sigma_A$
A	E	4.3	$\sigma_A$
E	B	4.3	$\sigma_E$



← coin-flip →



## Zerocash

zero knowledge proofs + Bitcoin

1. Alice owns coin  $c_1$  with comm  $cm_1$ .
2. To pay Bob, Alice:



$pk_A, sk_A$



Ledger		
Old	New	Proof
		⋮
8436378	$cm_1$	$\pi_1$
6327690	$cm_2$	$\pi_2$

$pk_B, sk_B$



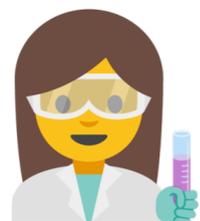
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From	To	Amt	Sign
		⋮	
M	N	2.3	$\sigma_M$
A	M	10	$\sigma_A$
A	E	4.3	$\sigma_A$
E	B	4.3	$\sigma_E$



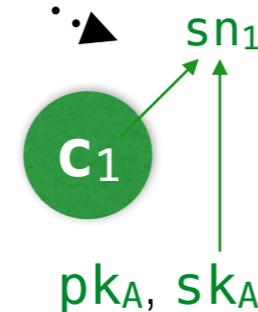
← coin-flip →



## Zerocash

zero knowledge proofs + Bitcoin

1. Alice owns coin  $c_1$  with comm  $cm_1$ .
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  - a) derives  $sn_1$  from  $c_1$  and  $sk_A$ .



Ledger		
Old	New	Proof
		⋮
8436378	$cm_1$	$\pi_1$
6327690	$cm_2$	$\pi_2$



$pk_B, sk_B$



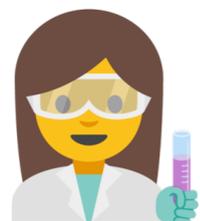
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Ledger			
From	To	Amt	Sign
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M	N	2.3	$\sigma_M$
A	M	10	$\sigma_A$
A	E	4.3	$\sigma_A$
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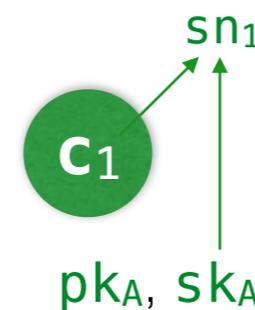
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zero knowledge proofs + Bitcoin

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8436378	$cm_1$	$\pi_1$
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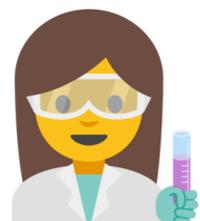
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M	N	2.3	$\sigma_M$
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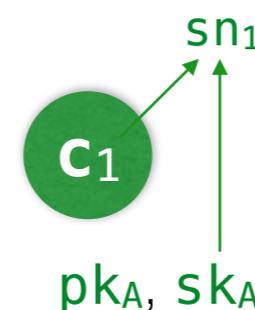
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  - c) creates ZK proof  $\pi_3$  for above.



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Old	New	Proof
		⋮
8436378	$cm_1$	$\pi_1$
6327690	$cm_2$	$\pi_2$

$pk_B, sk_B$



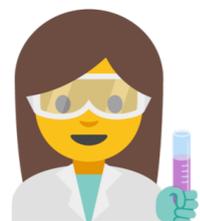
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M	N	2.3	$\sigma_M$
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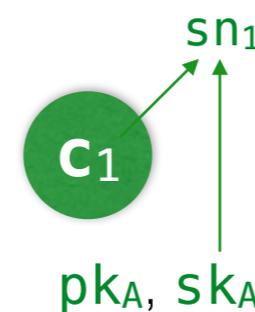
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  - d) appends tx =  $(sn_1, cm_3, \pi_3)$ .



Ledger		
Old	New	Proof
		⋮
8436378	$cm_1$	$\pi_1$
6327690	$cm_2$	$\pi_2$
$sn_1$	$cm_3$	$\pi_3$

$pk_B, sk_B$



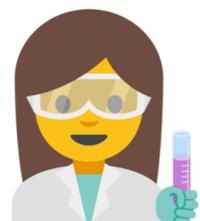
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M	N	2.3	$\sigma_M$
A	M	10	$\sigma_A$
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← coin-flip →

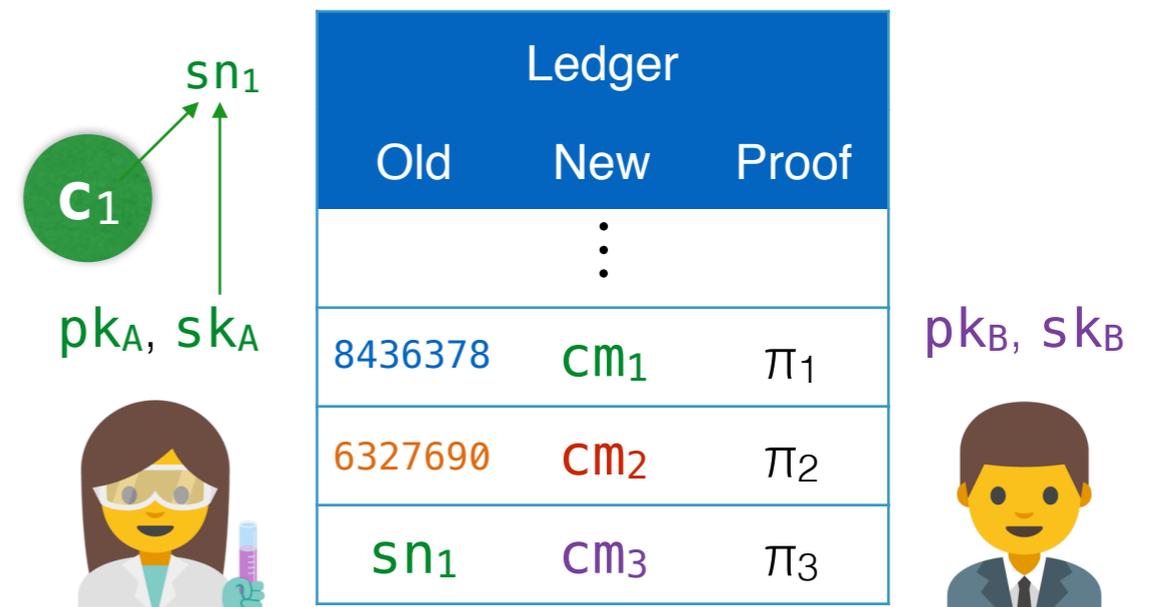


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  - d) appends tx =  $(sn_1, cm_3, \pi_3)$ .

Cannot link  $sn_1$  with  $cm_1$  without  $sk_A$ .



# Naive Attempt: PS + Zerocash

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Ledger		
Old	New	Proof
	⋮	
8436378	$cm_1$	$\pi_1$
6327690	$cm_2$	$\pi_2$



# Naive Attempt: PS + Zerocash

1. Alice escrows  $v$  in a Zerocash transaction. . .

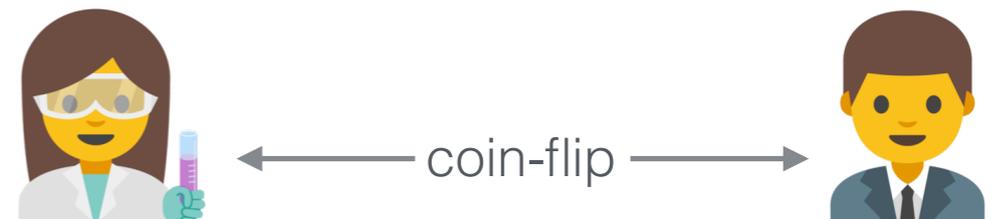
Ledger		
Old	New	Proof
	⋮	
8436378	$cm_1$	$\pi_1$
6327690	$cm_2$	$\pi_2$
$sn_1$	$cm_3$	$\pi_3$



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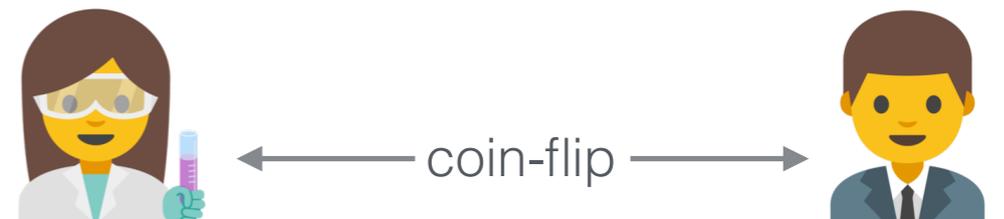
Ledger		
Old	New	Proof
	⋮	
8436378	CM <sub>1</sub>	$\pi_1$
6327690	CM <sub>2</sub>	$\pi_2$
SN <sub>1</sub>	CM <sub>3</sub>	$\pi_3$



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← coin-flip →

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8436378	CM <sub>1</sub>	$\pi_1$
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SN <sub>1</sub>	CM <sub>3</sub>	$\pi_3$
SN <sub>3</sub>	CM <sub>4</sub>	$\pi_4$

Major Issues:

**Linkability**

**Double Spending**

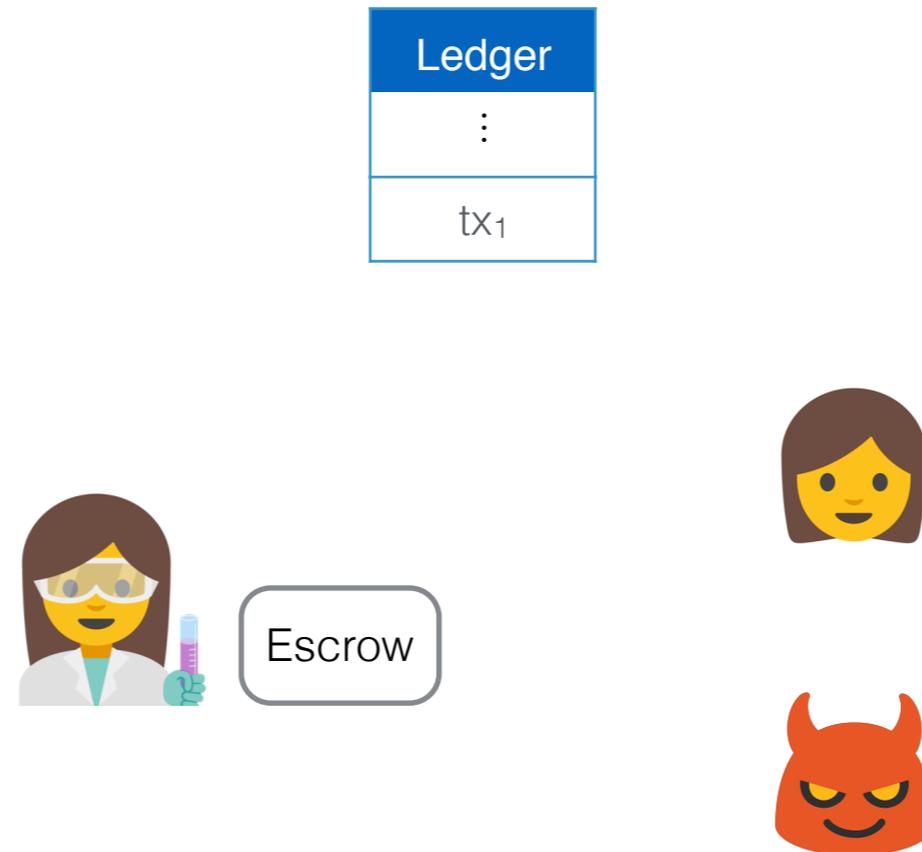


← coin-flip →



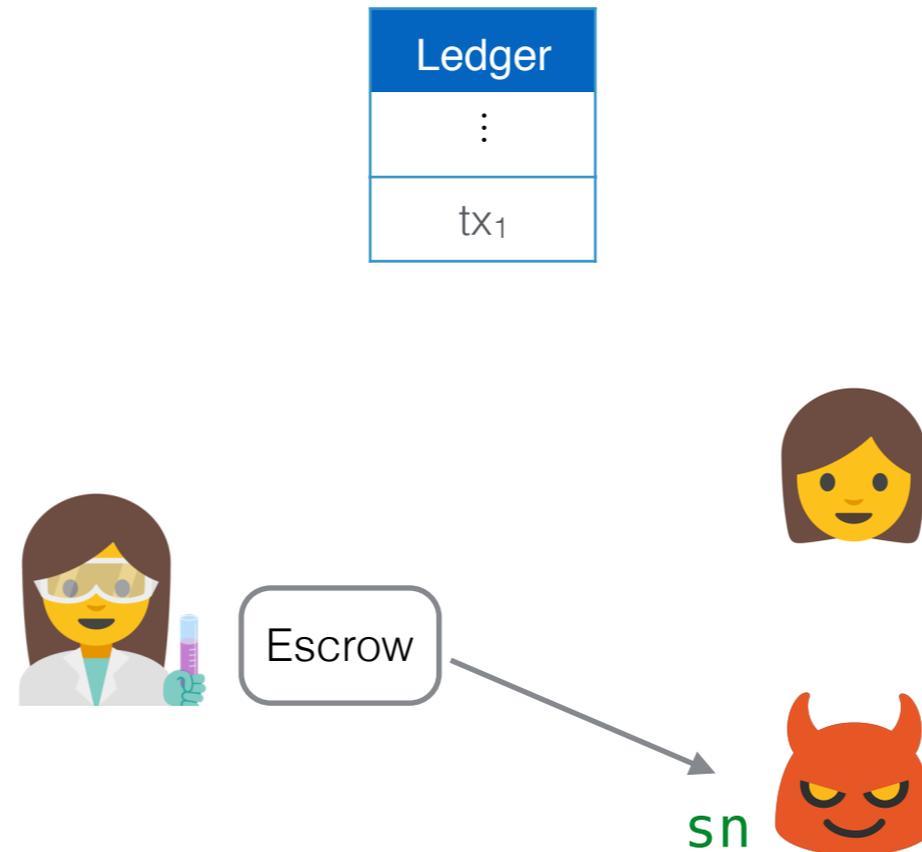
# Problem 1: Linkability

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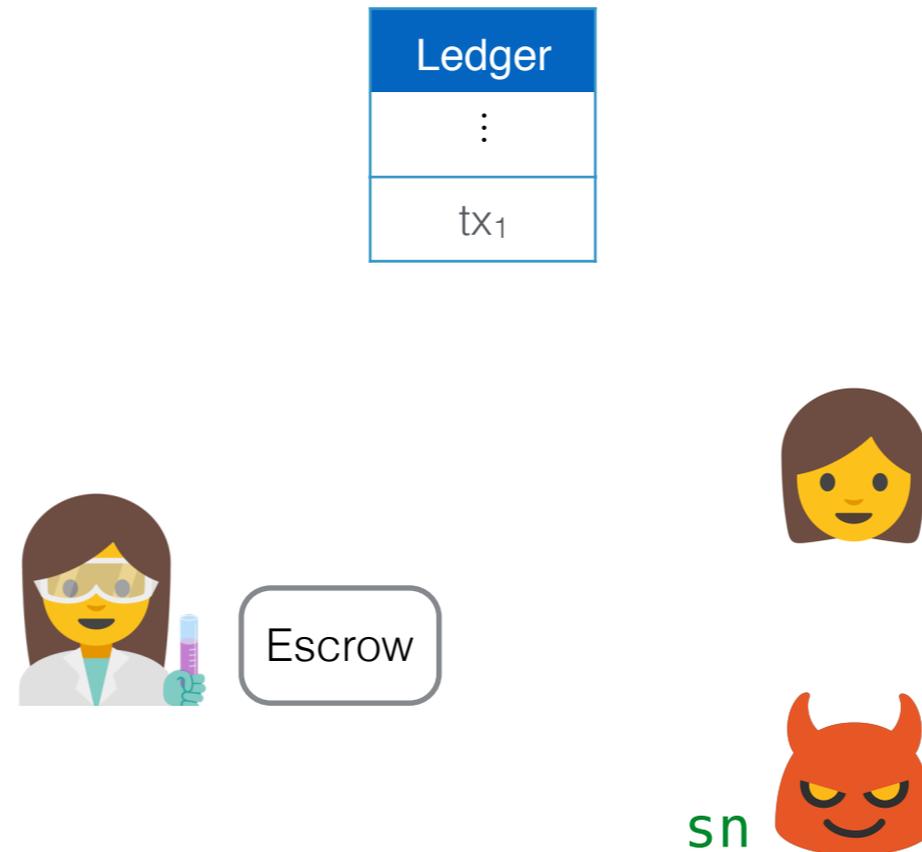
- To amortize transaction fees, Alice has to reuse escrow.
- Bob **always** learns serial number of escrowed coin.

# Problem 1: Linkability



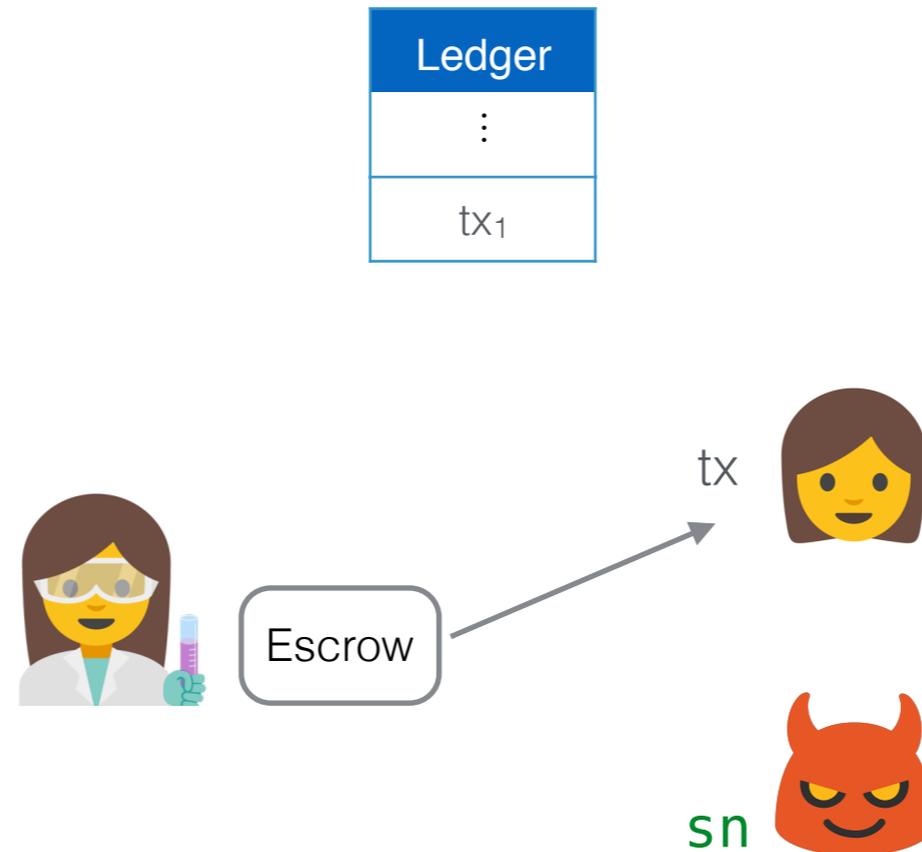
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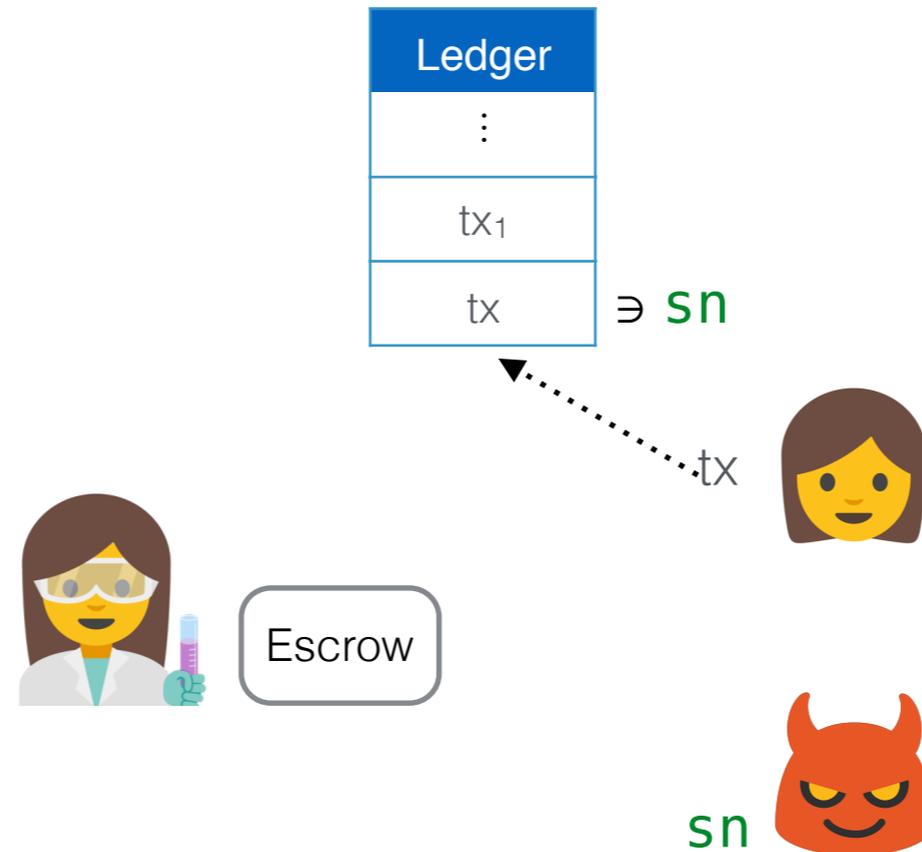
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- To amortize transaction fees, Alice has to reuse escrow.
- Bob **always** learns serial number of escrowed coin.
  - Can track Alice when she spends coin w/ others.
- Further attacks lead to loss of most privacy.

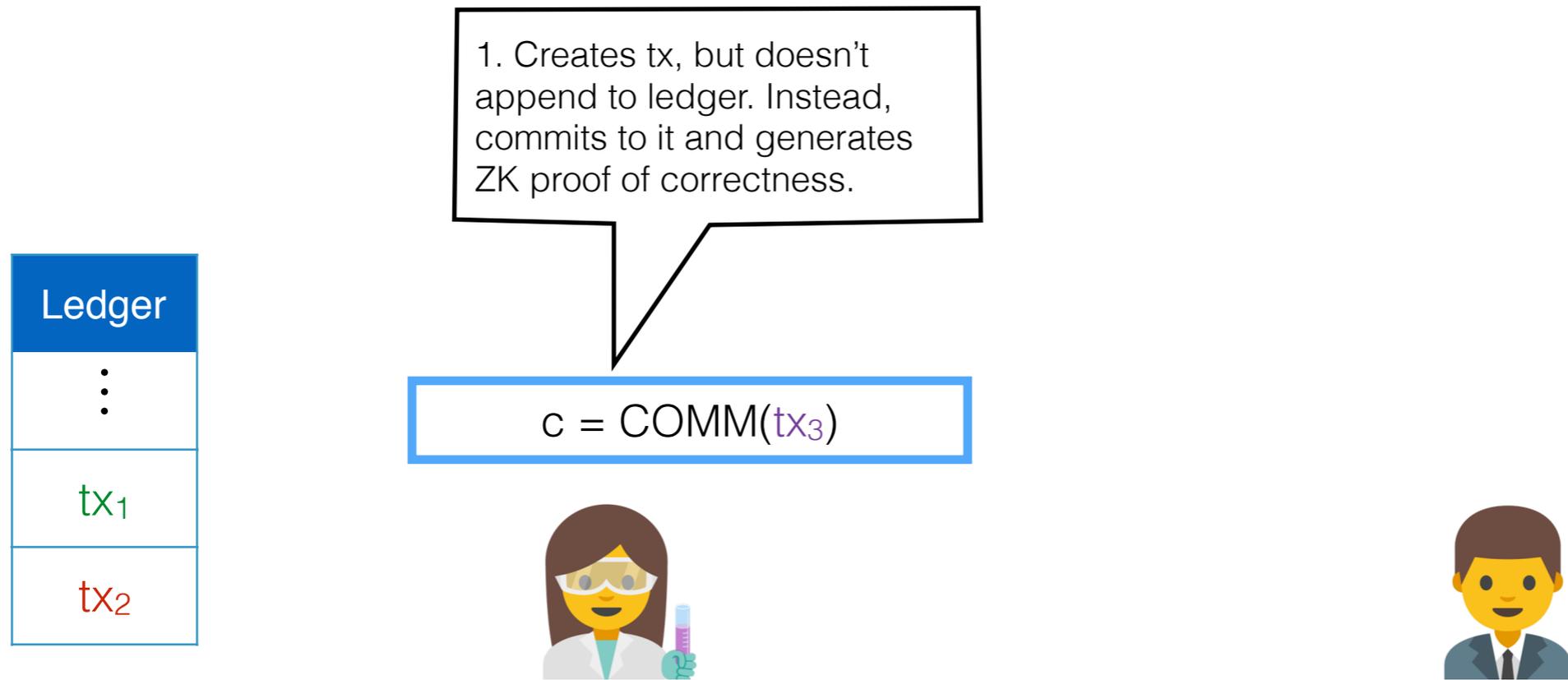
Solution: Make `sn` translucent

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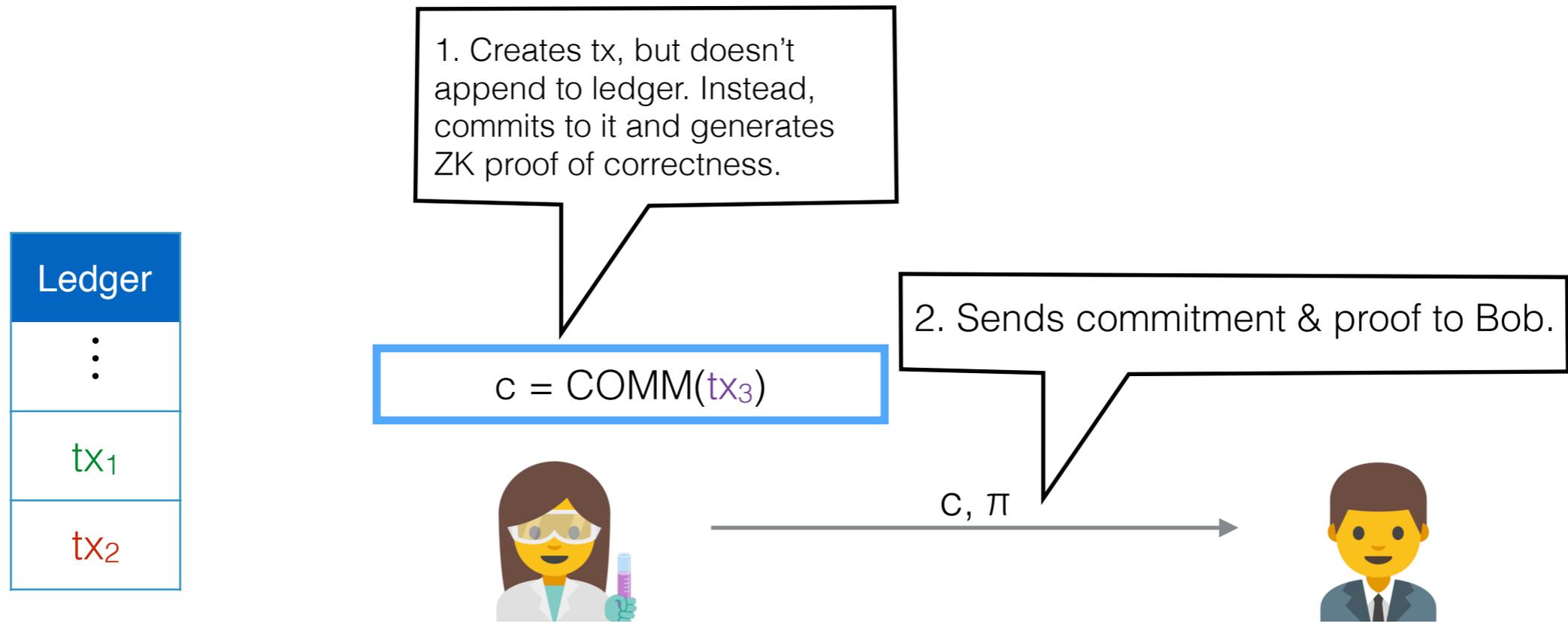
Ledger
⋮
tx <sub>1</sub>
tx <sub>2</sub>



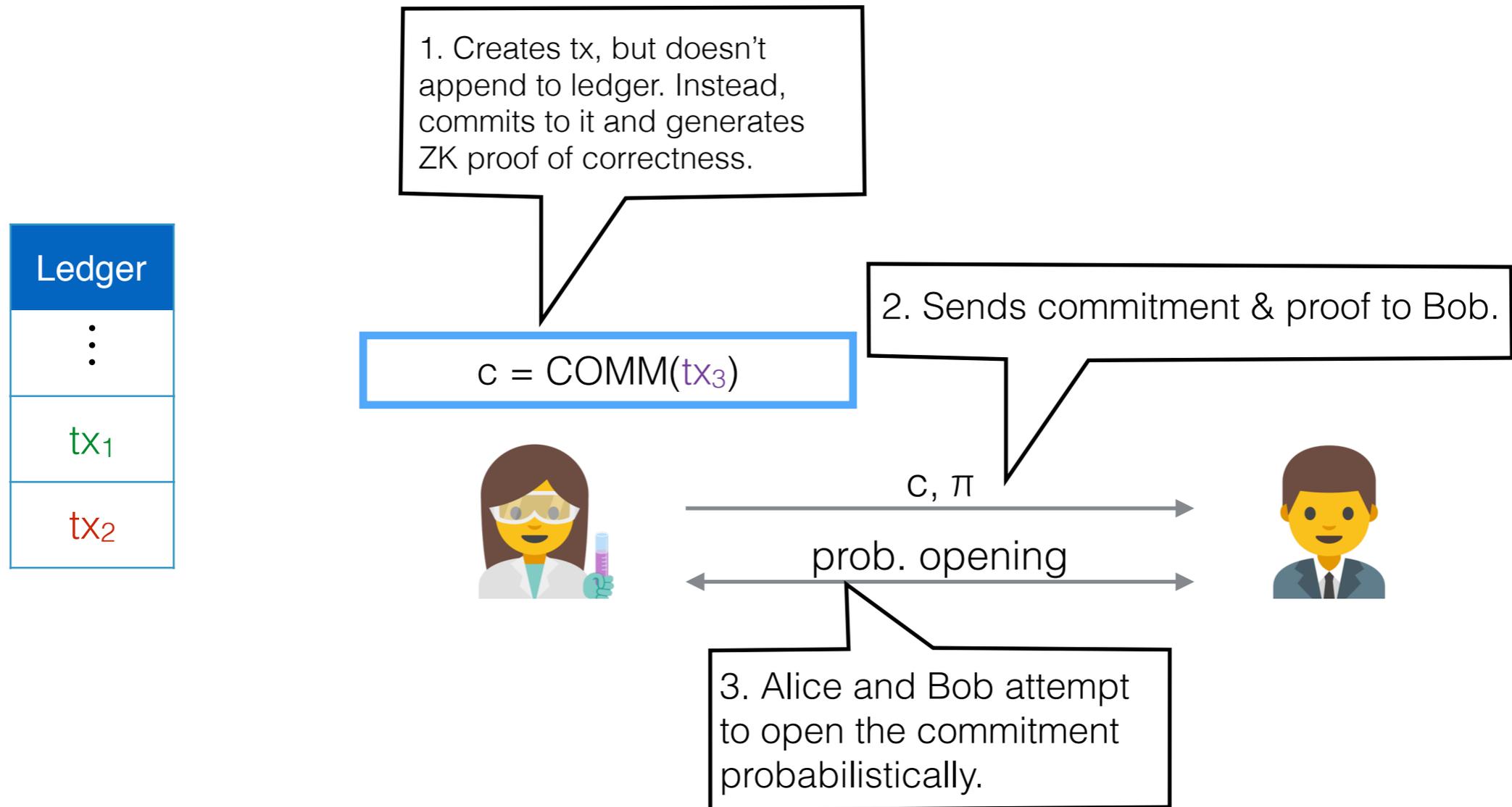
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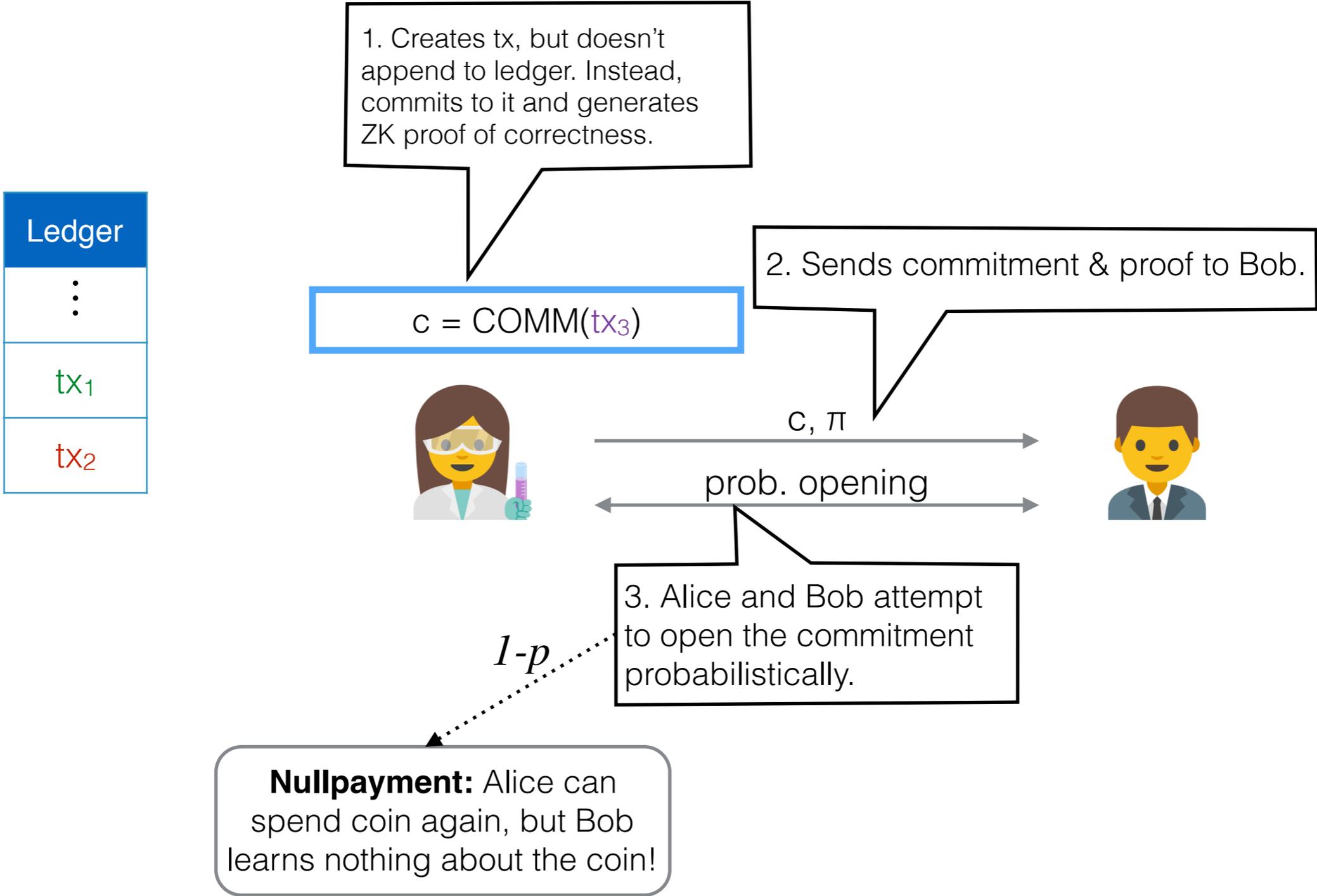
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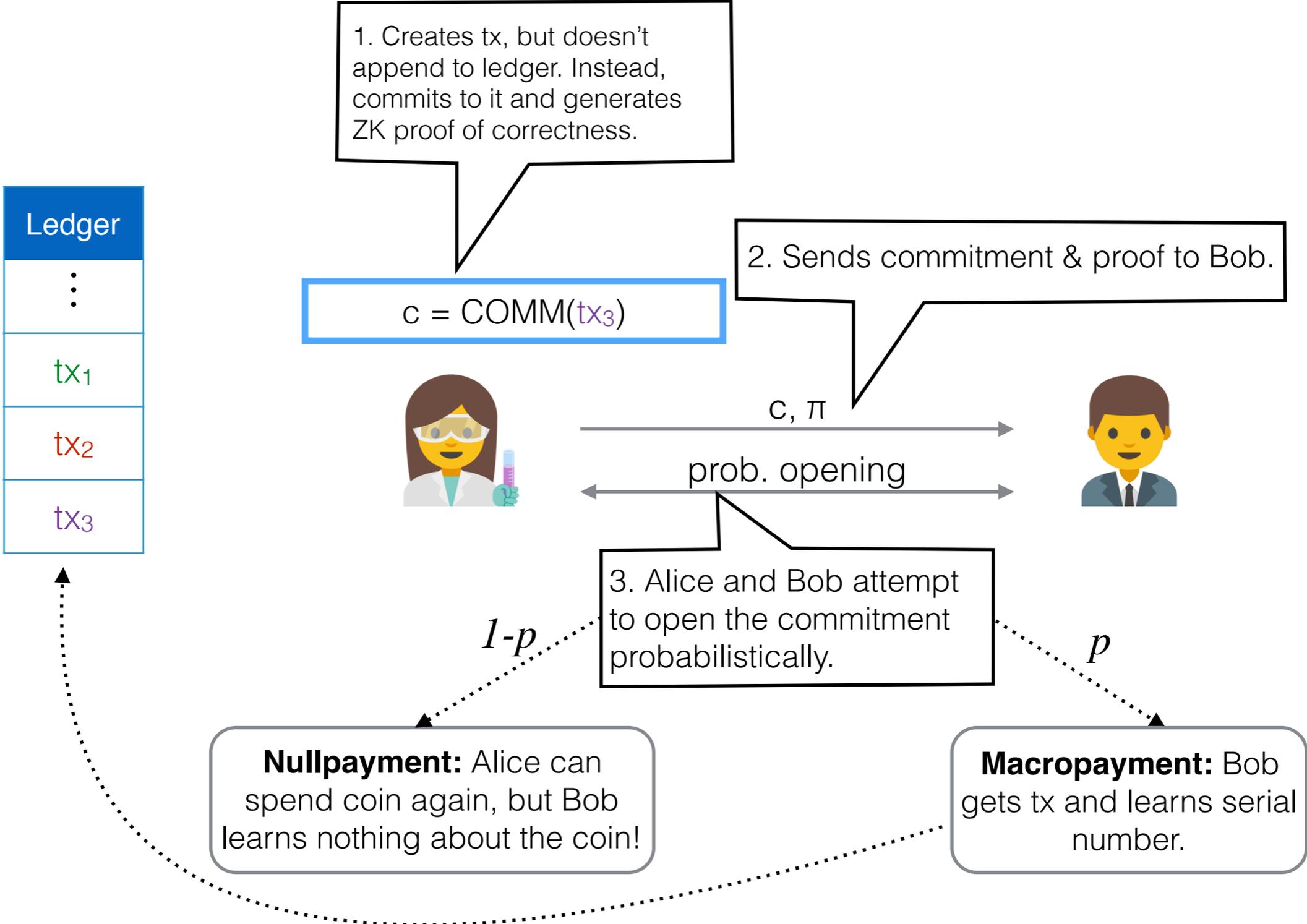
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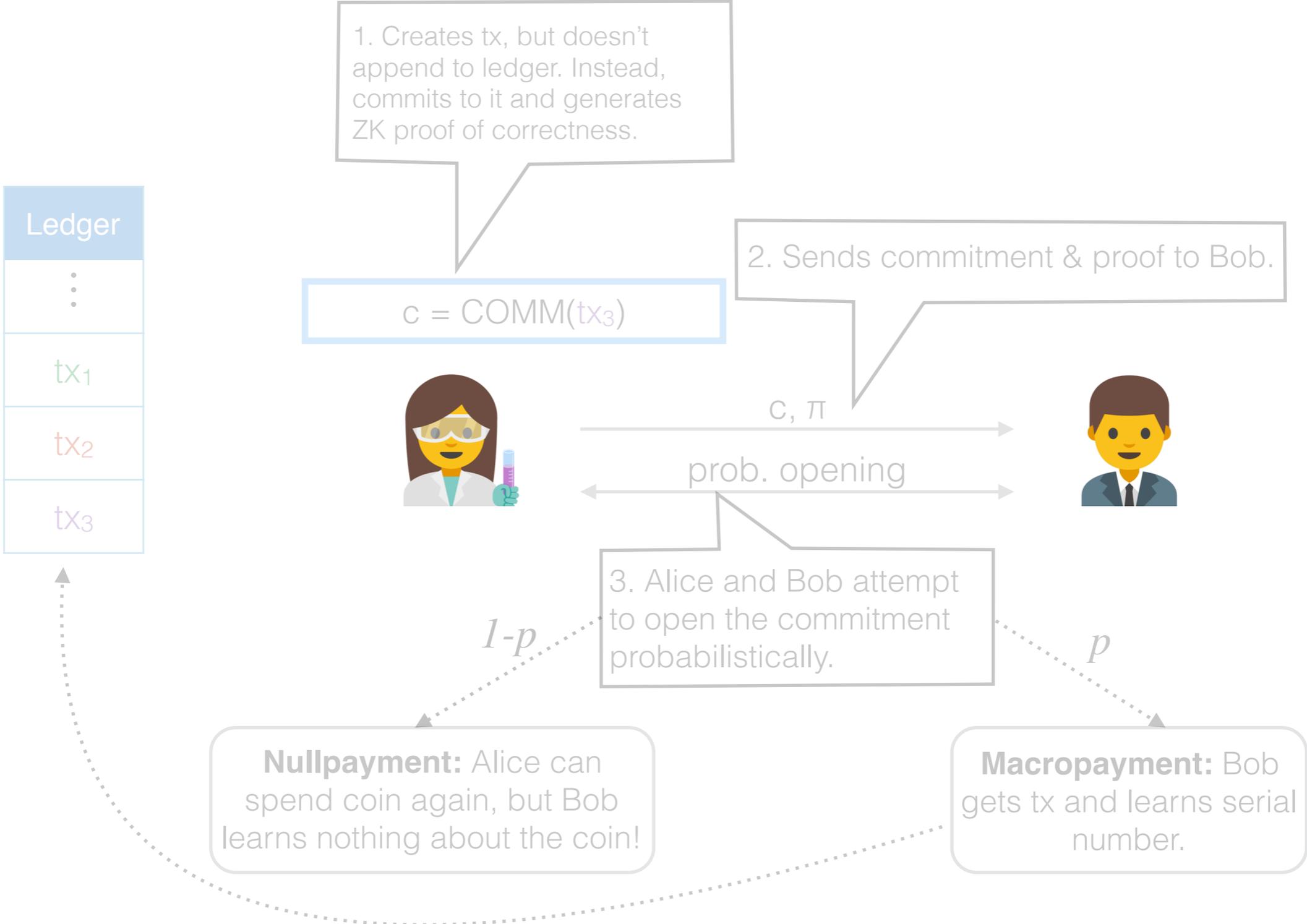
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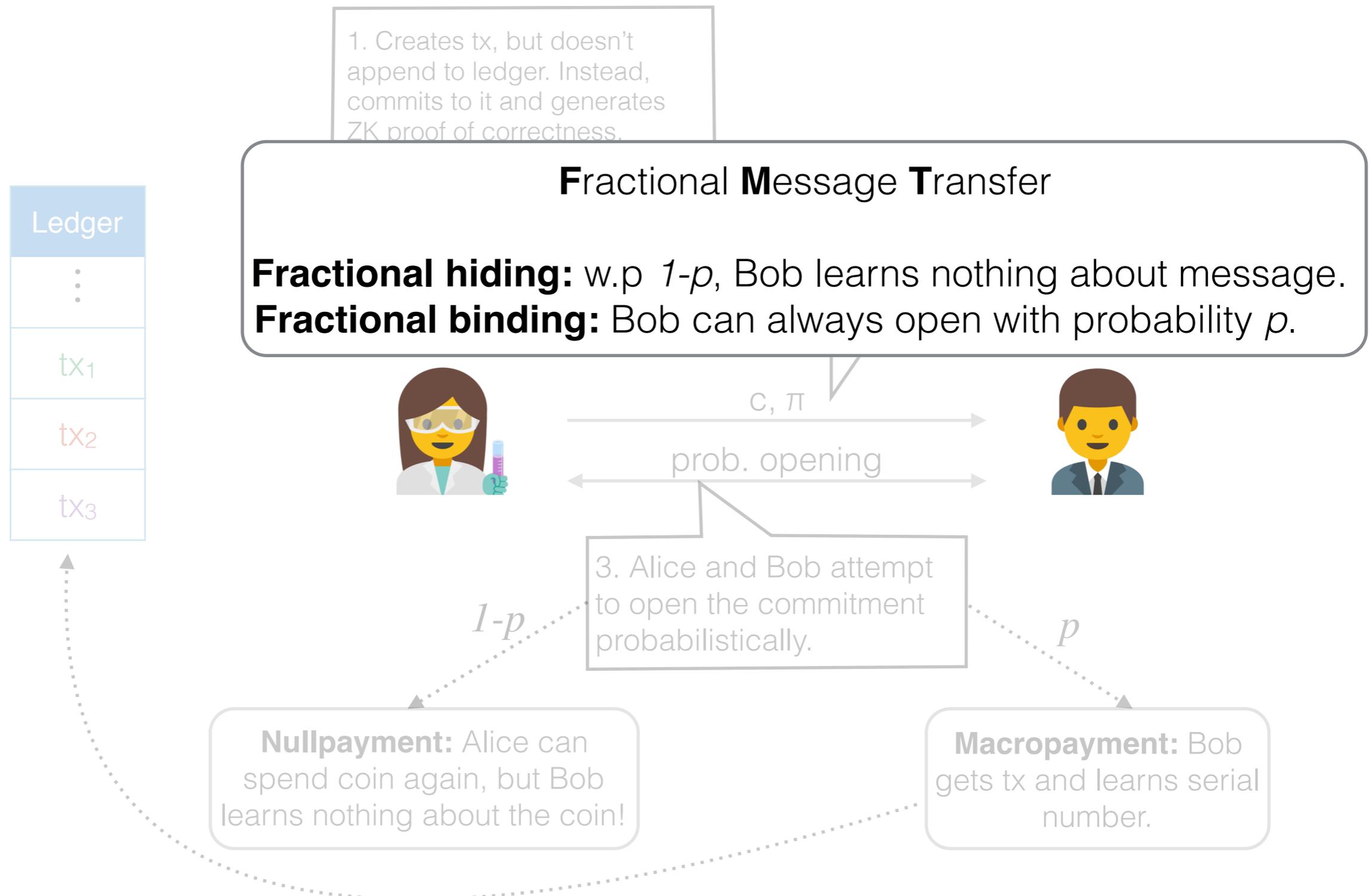
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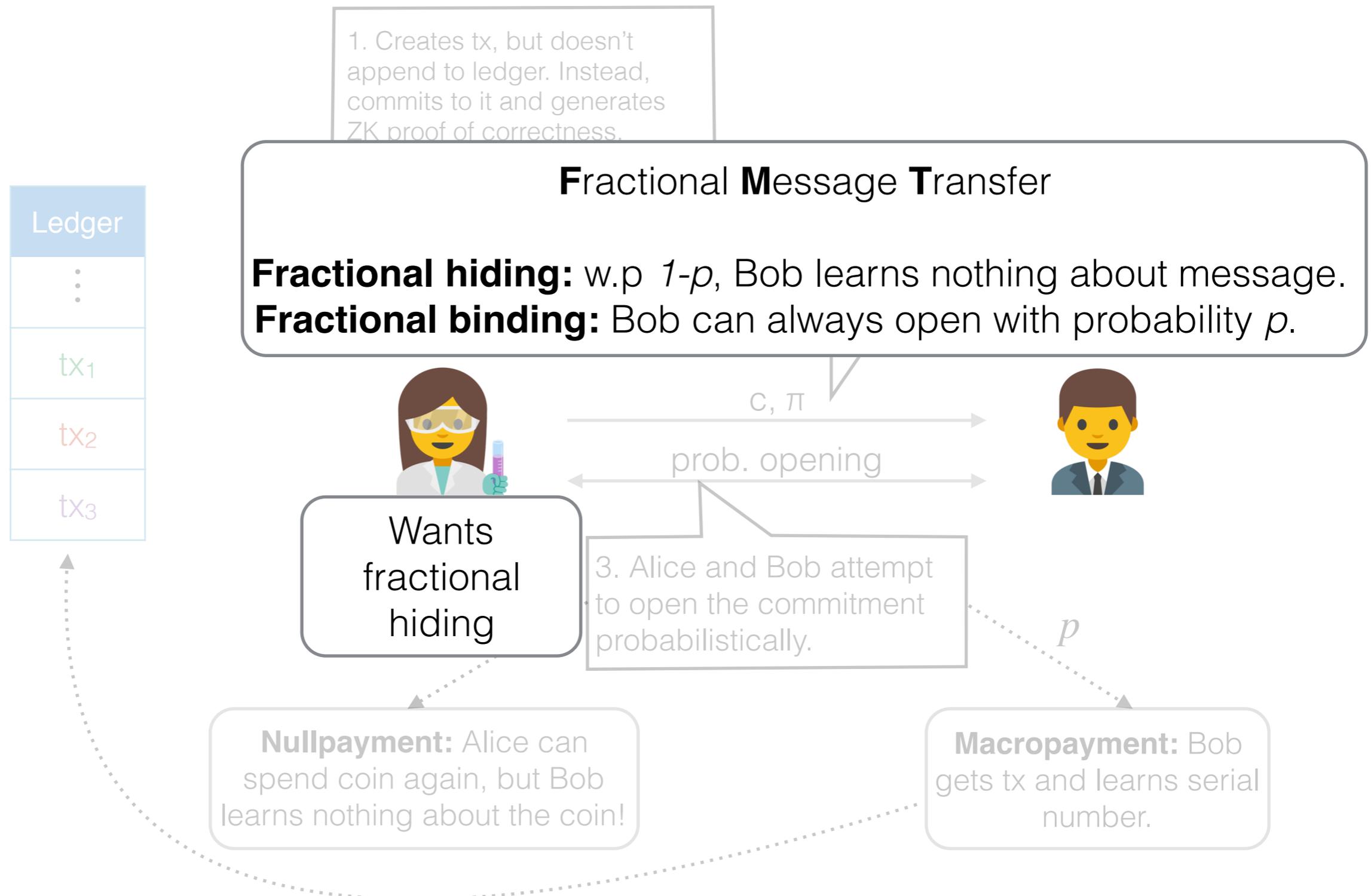
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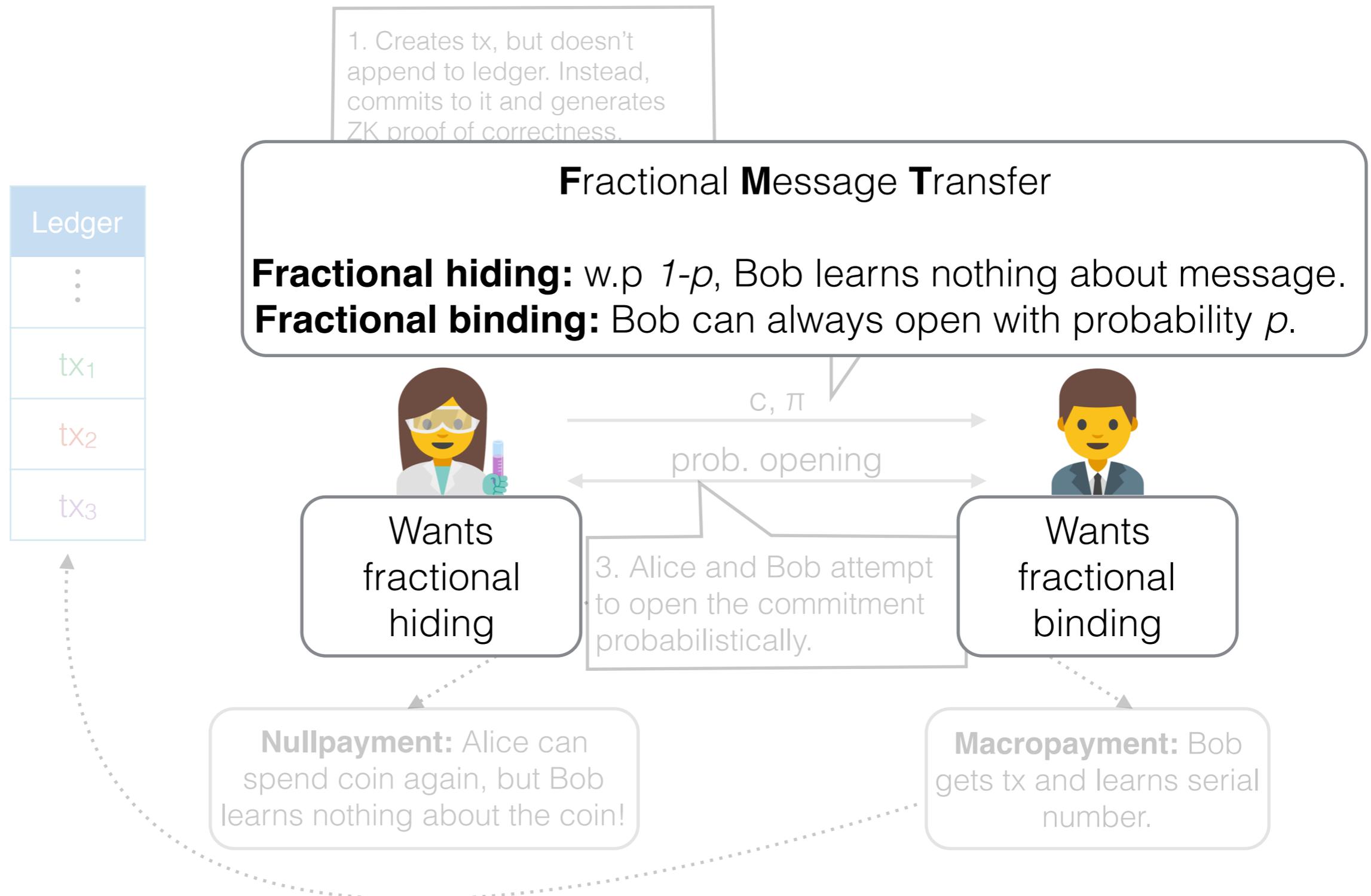
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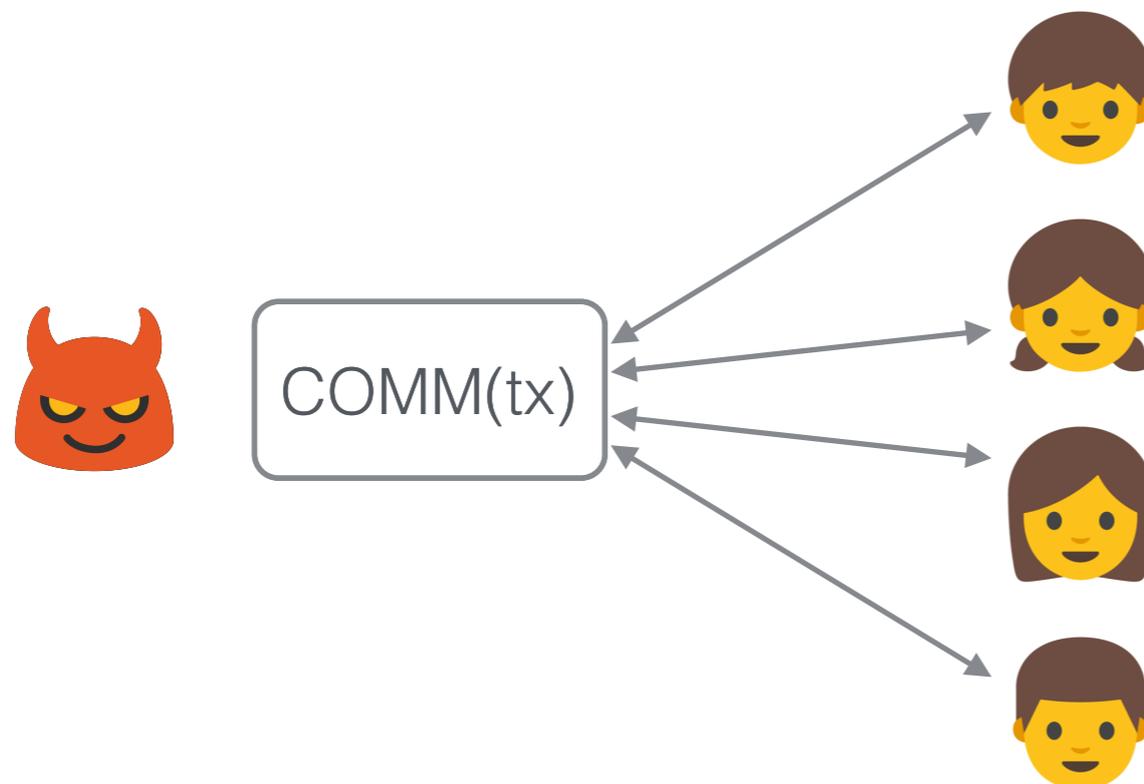
# Problem 2: Double-Spending

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Malice can use the same coin in multiple payments **in parallel**.

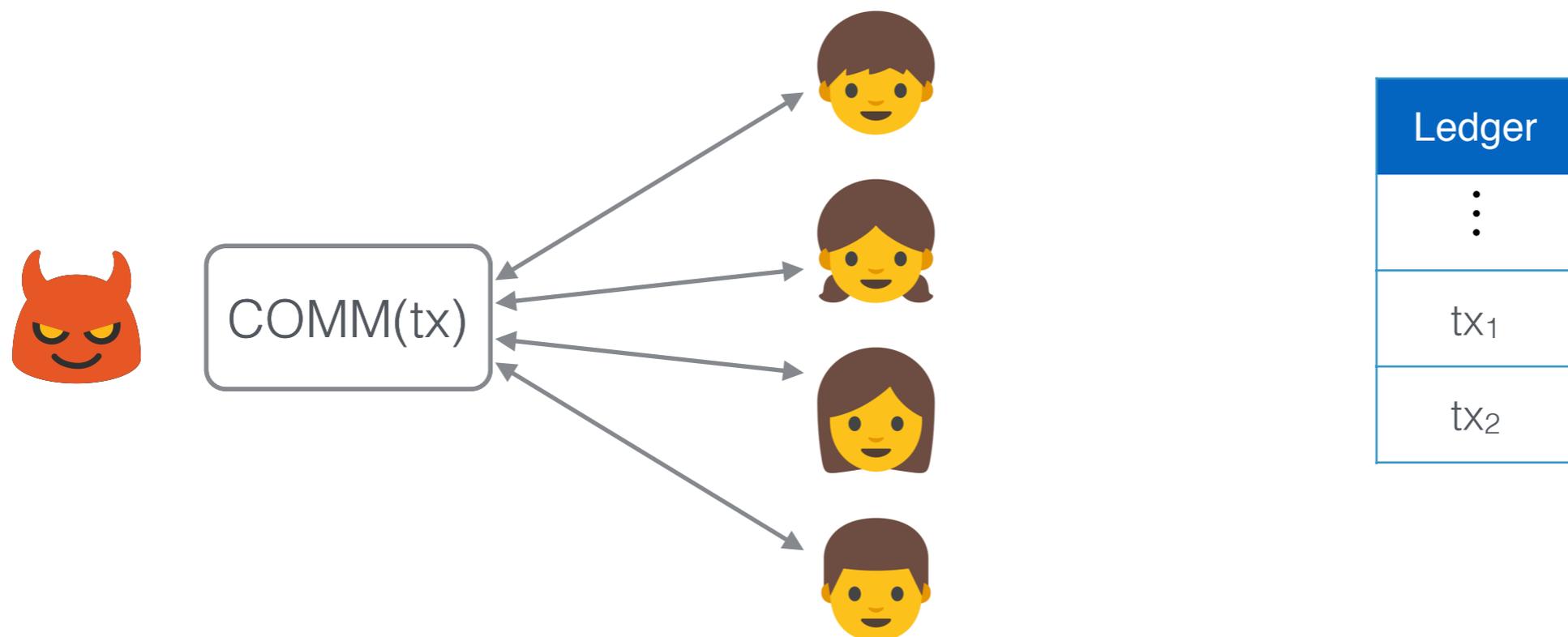
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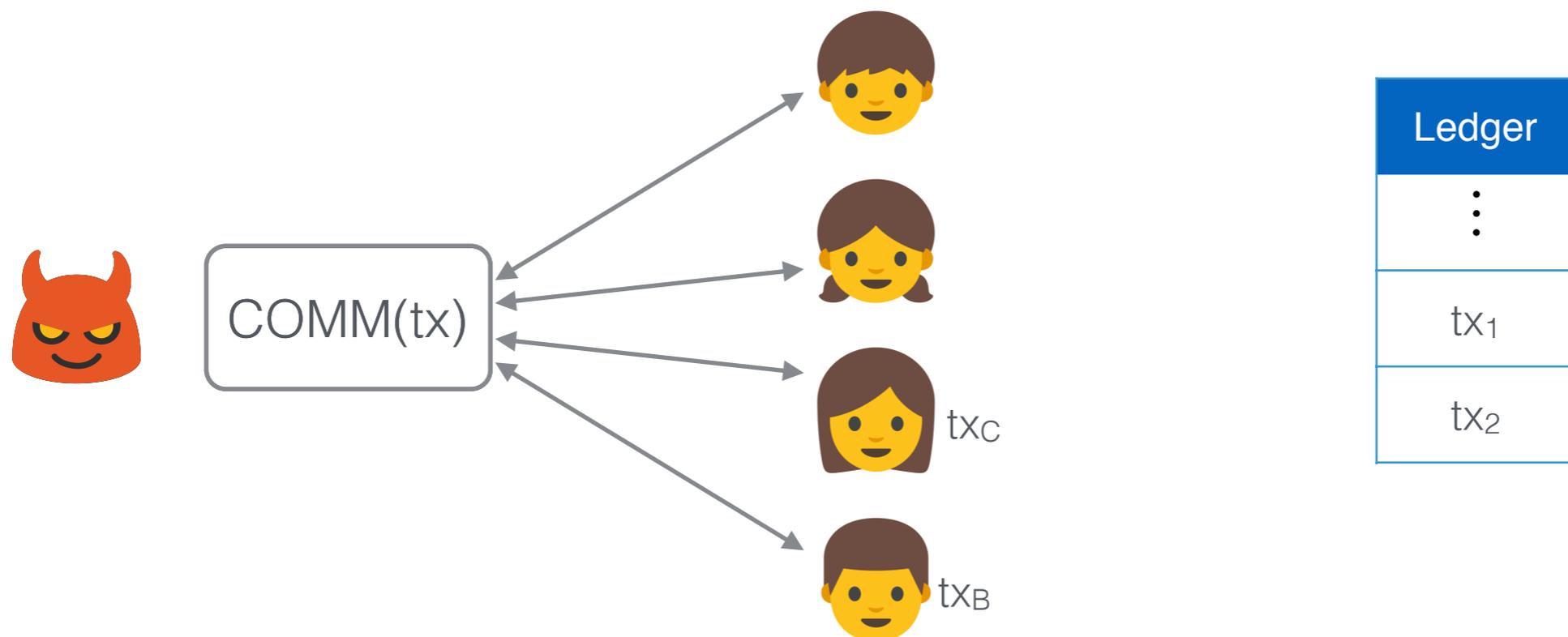
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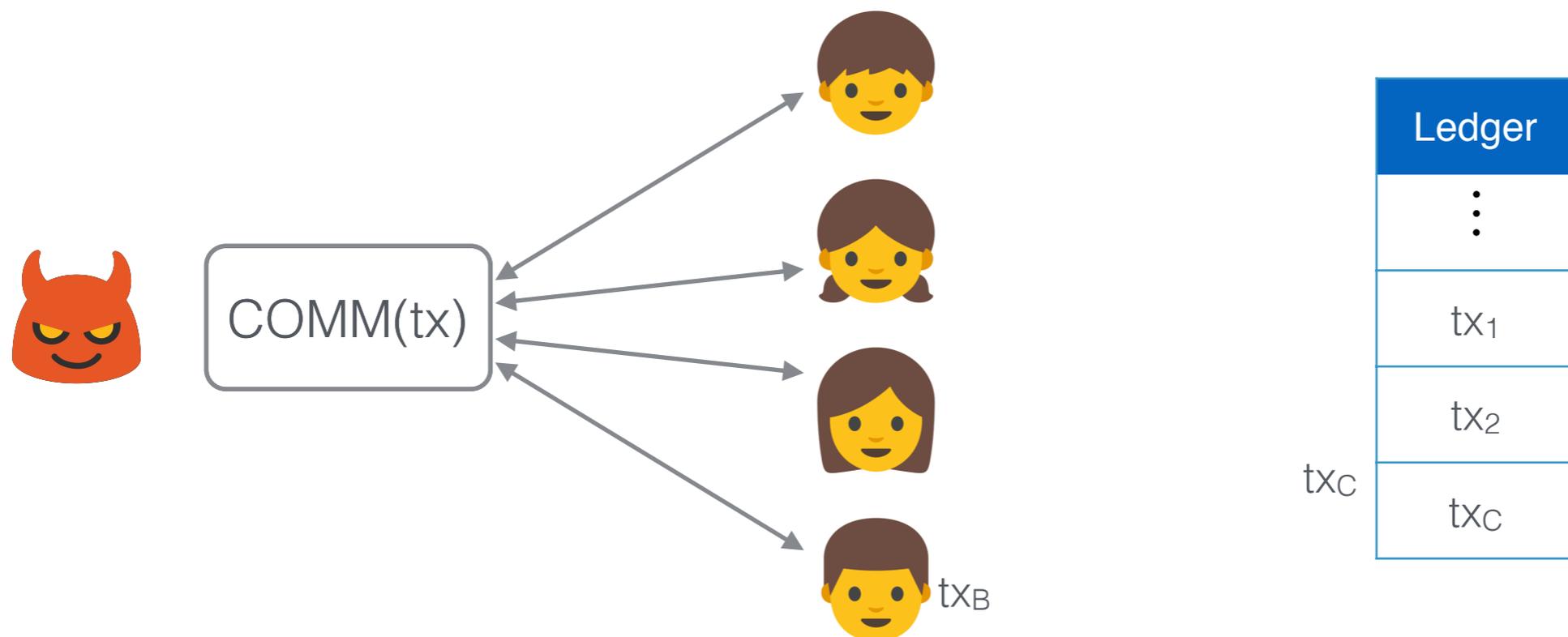
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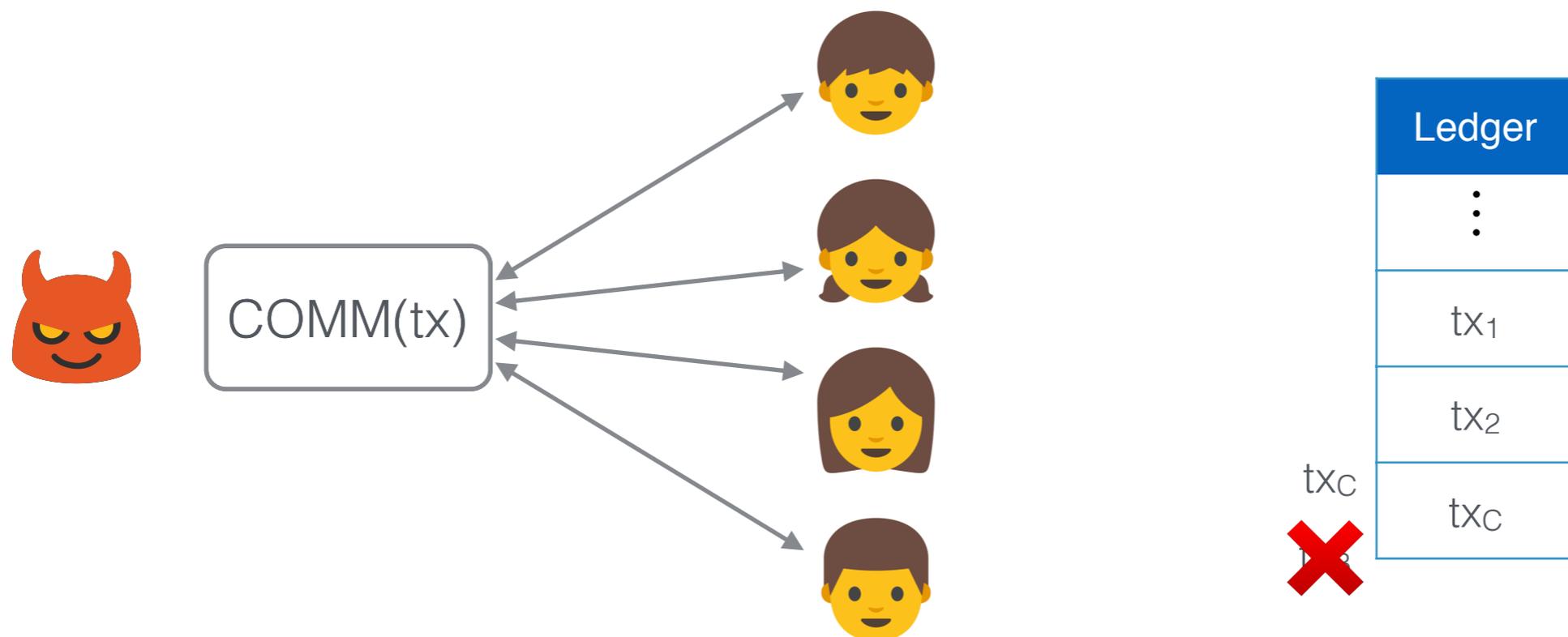
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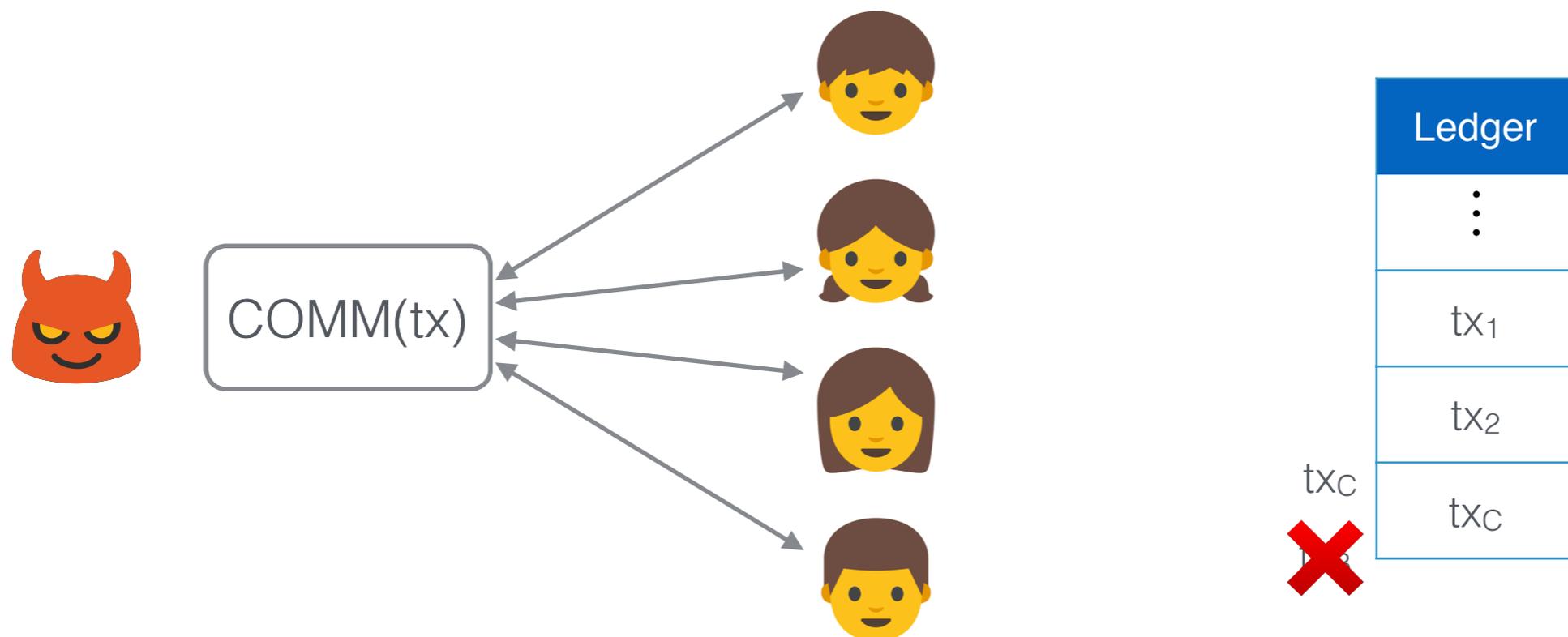
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# Problem 2: Double-Spending

Malice can use the same coin in multiple payments **in parallel**.

Offline setting  $\Rightarrow$  such attacks **cannot be prevented**.



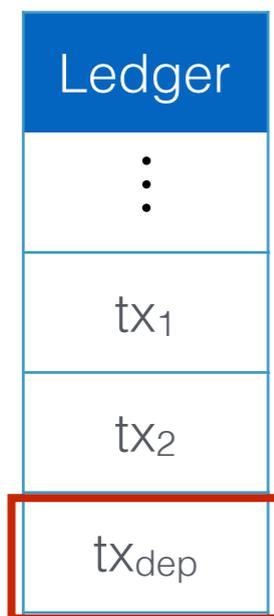
Solution: deposits + rationality

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Ledger
⋮
tx <sub>1</sub>
tx <sub>2</sub>

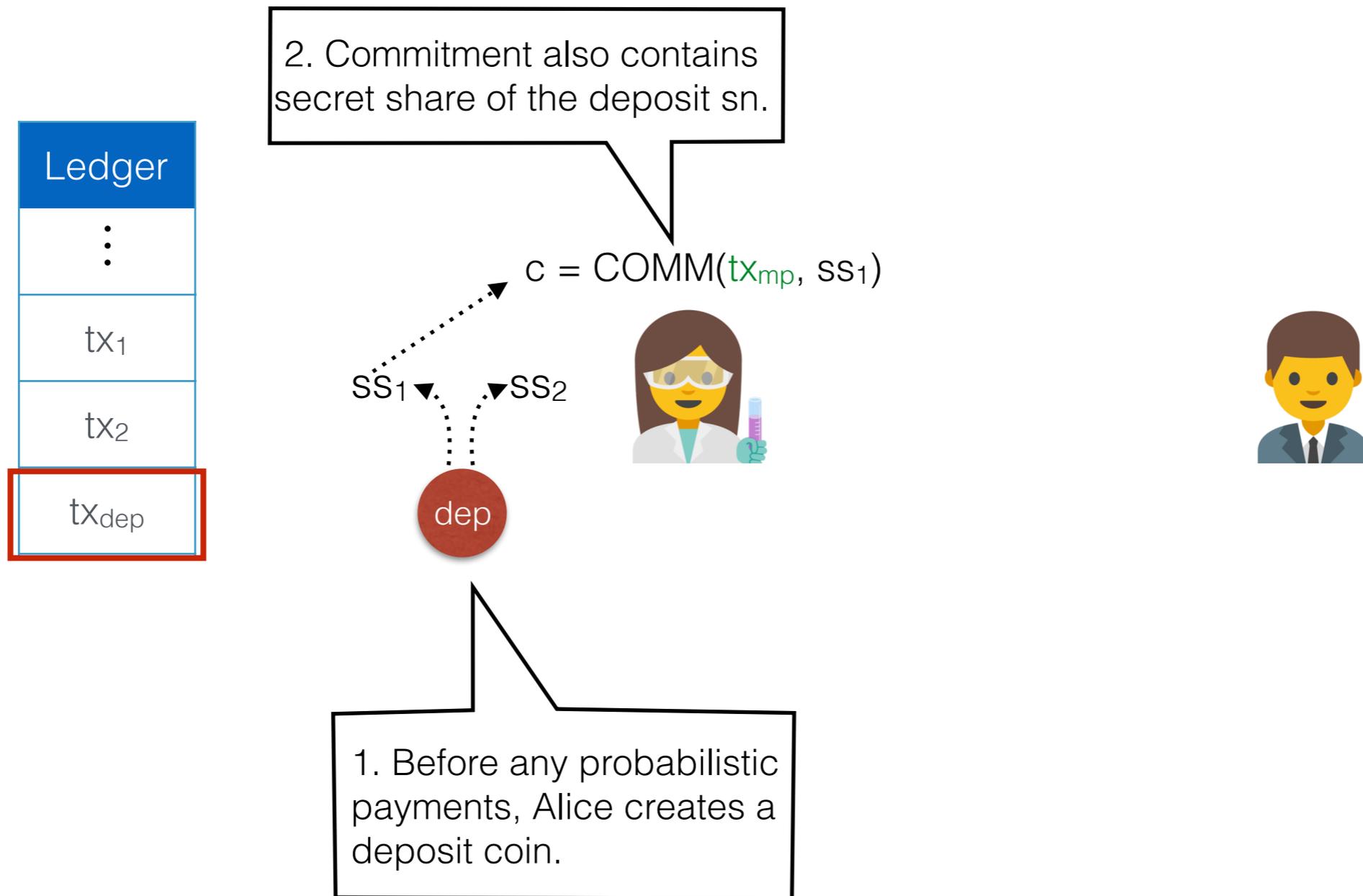


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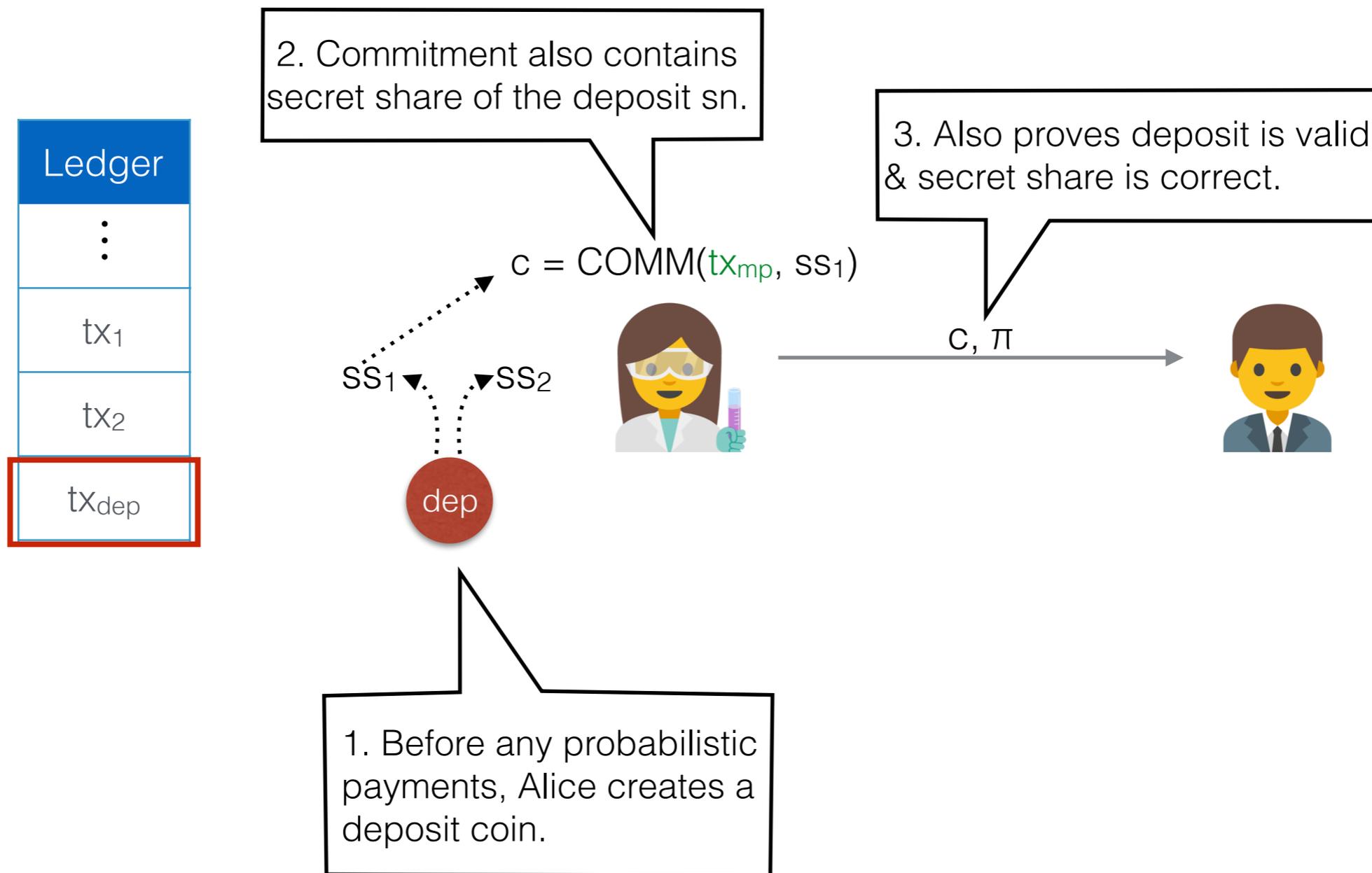


1. Before any probabilistic payments, Alice creates a deposit coin.

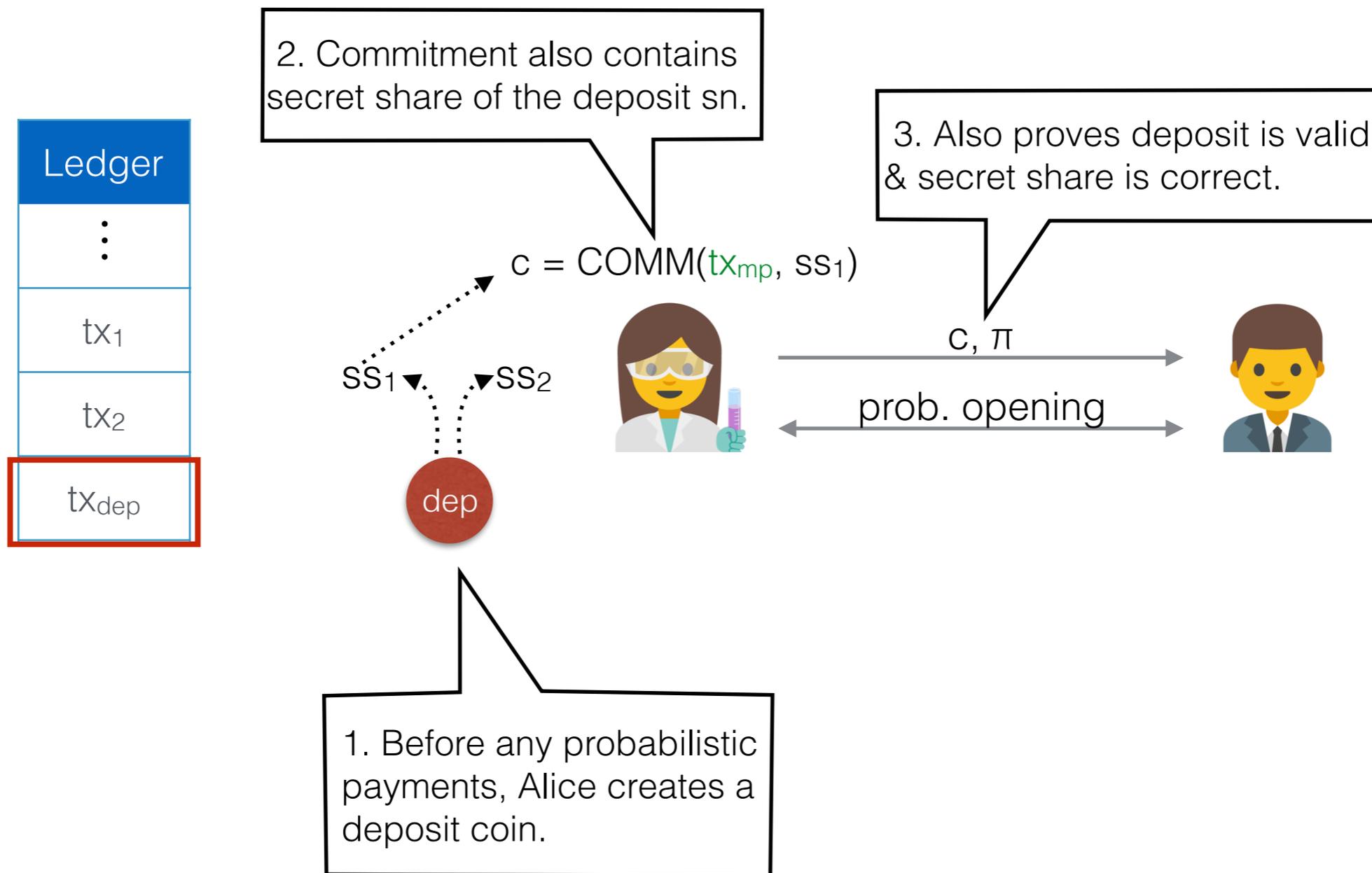
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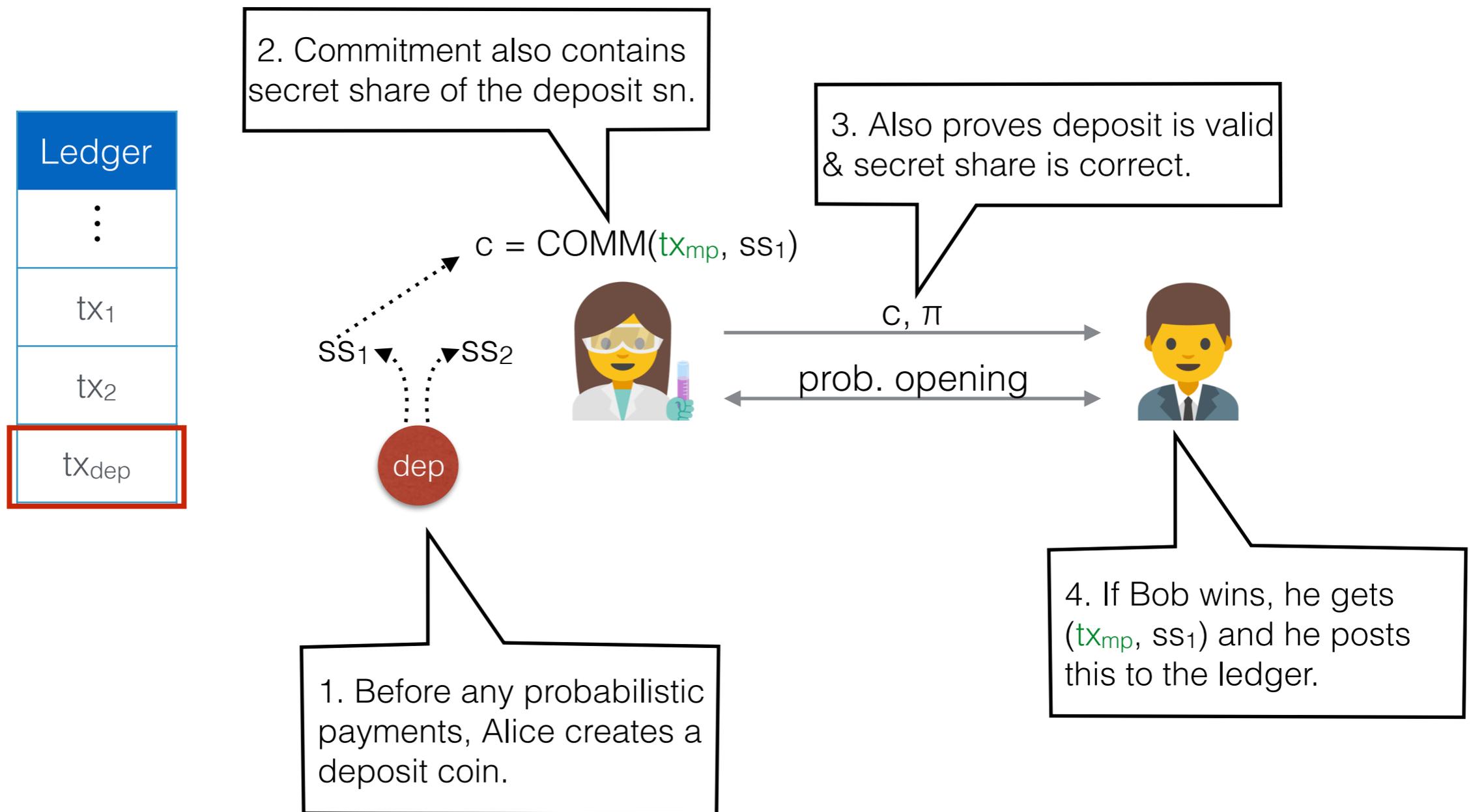
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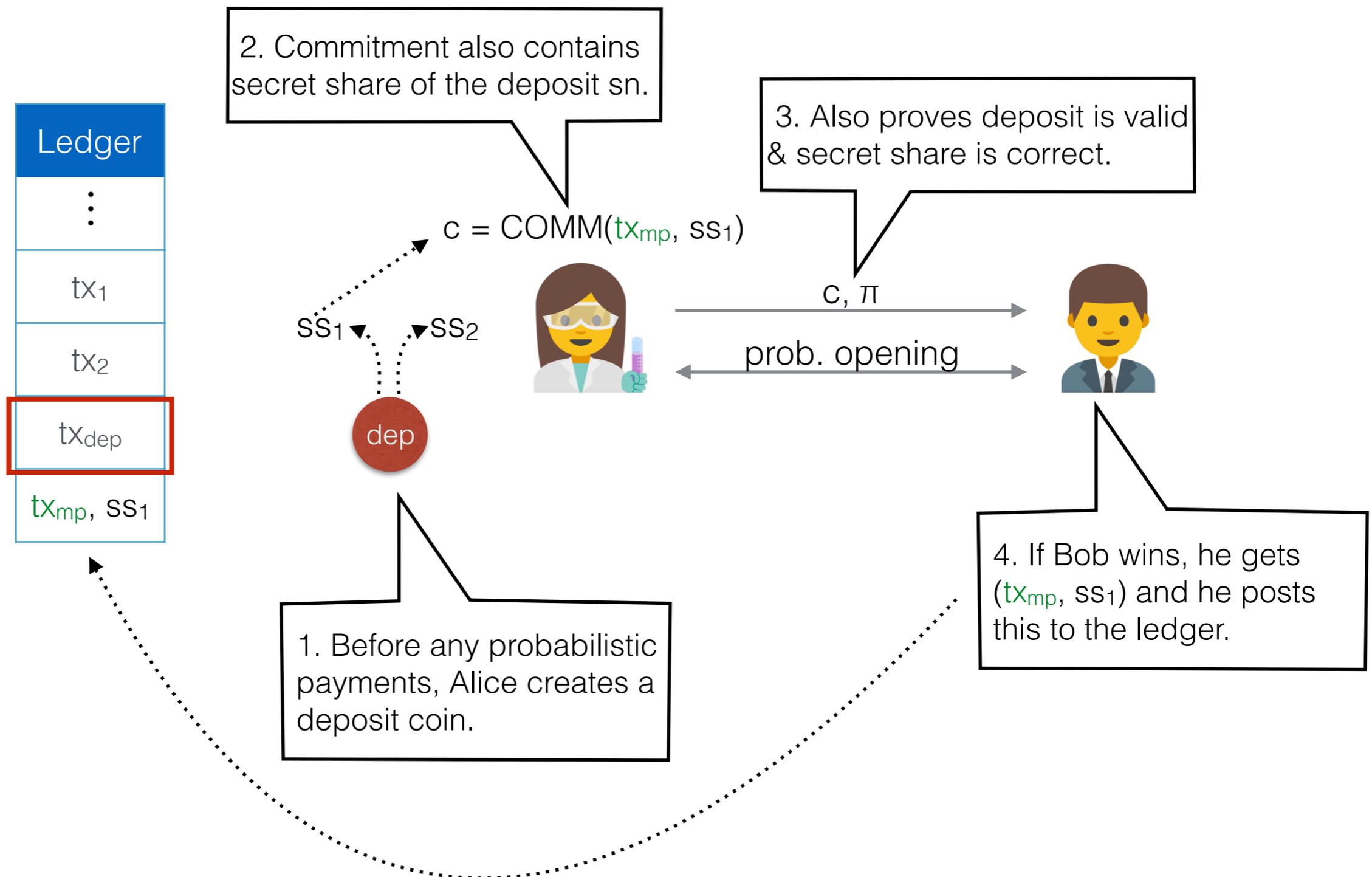
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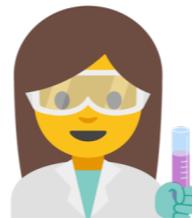
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⋮
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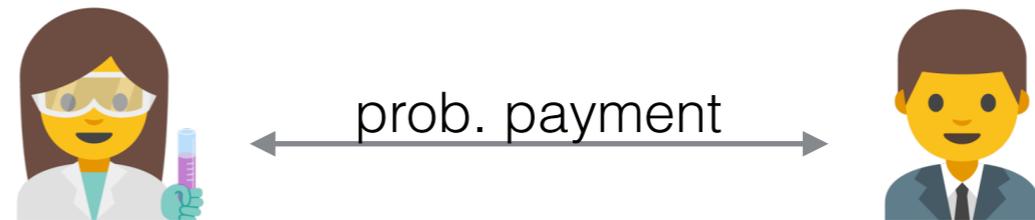
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⋮
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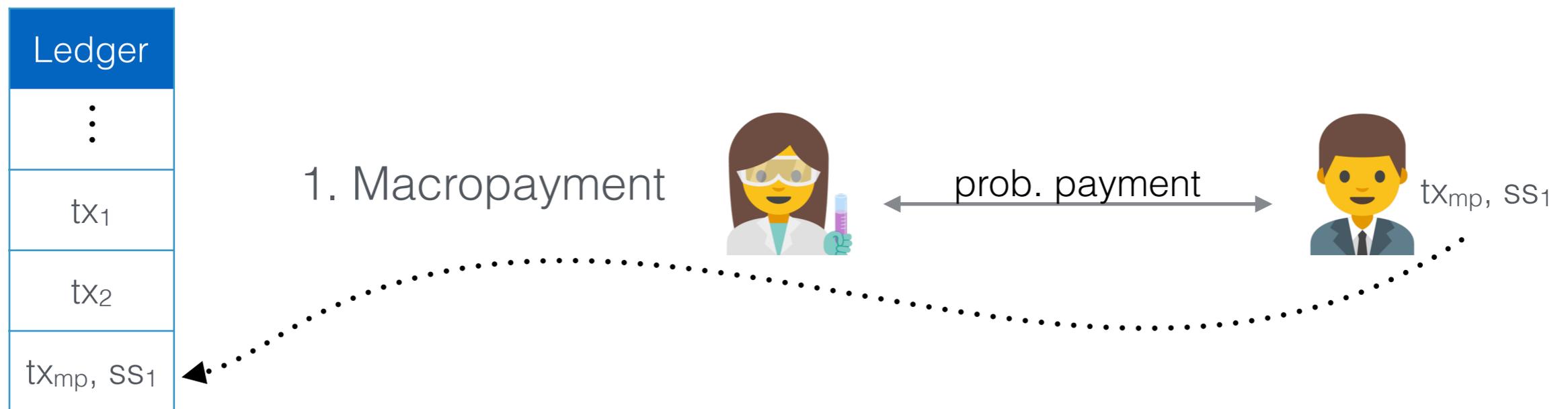


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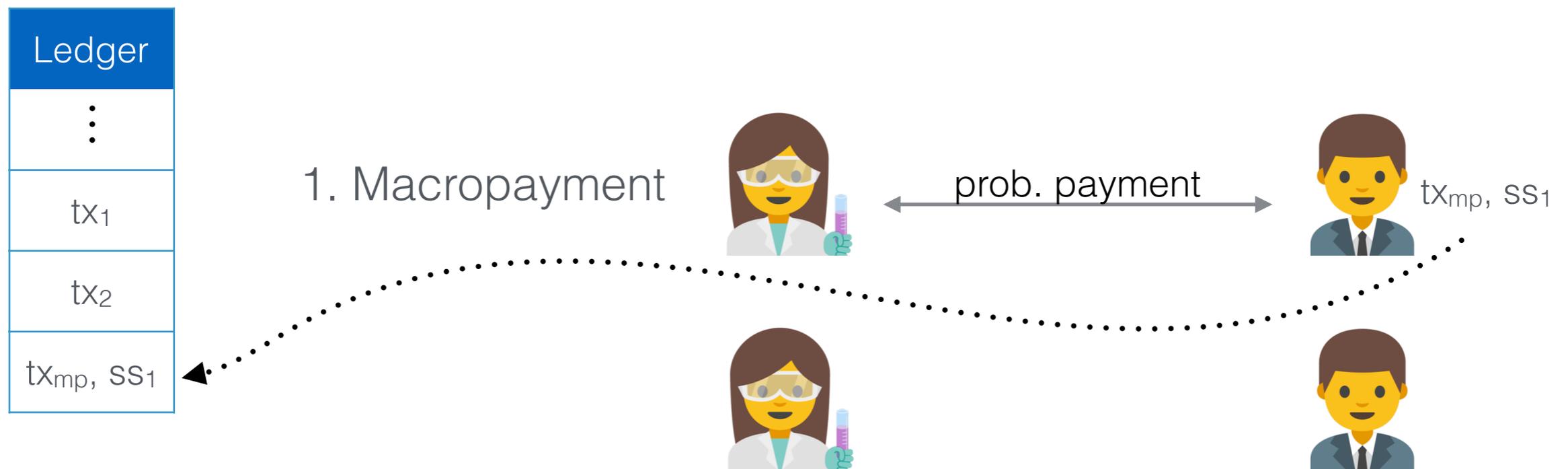
Ledger
⋮
tx <sub>1</sub>
tx <sub>2</sub>



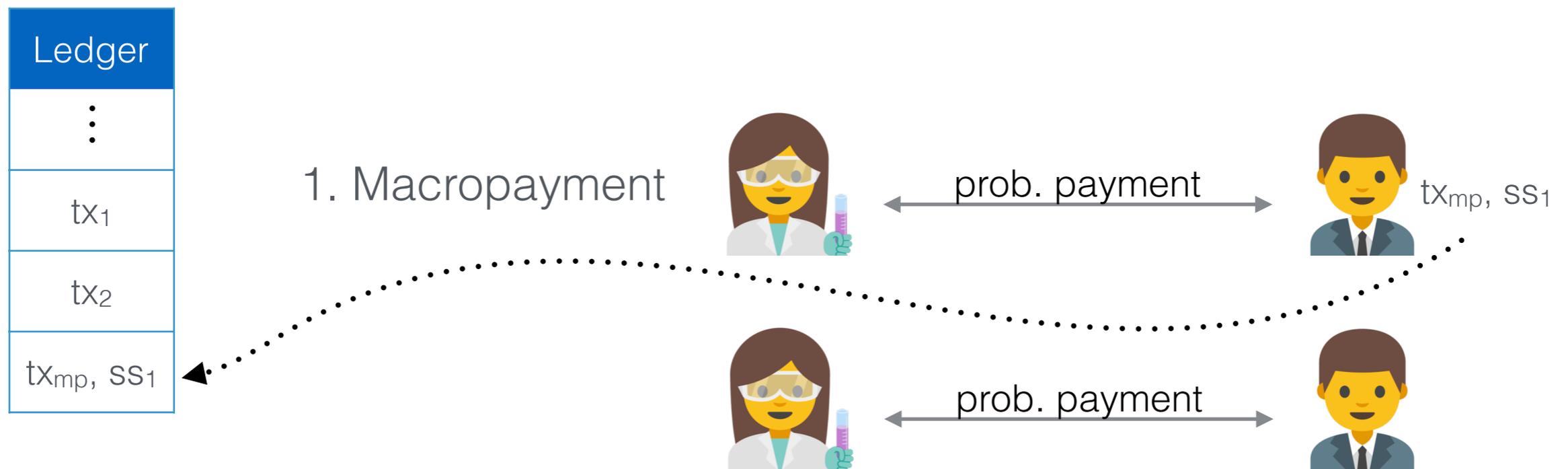
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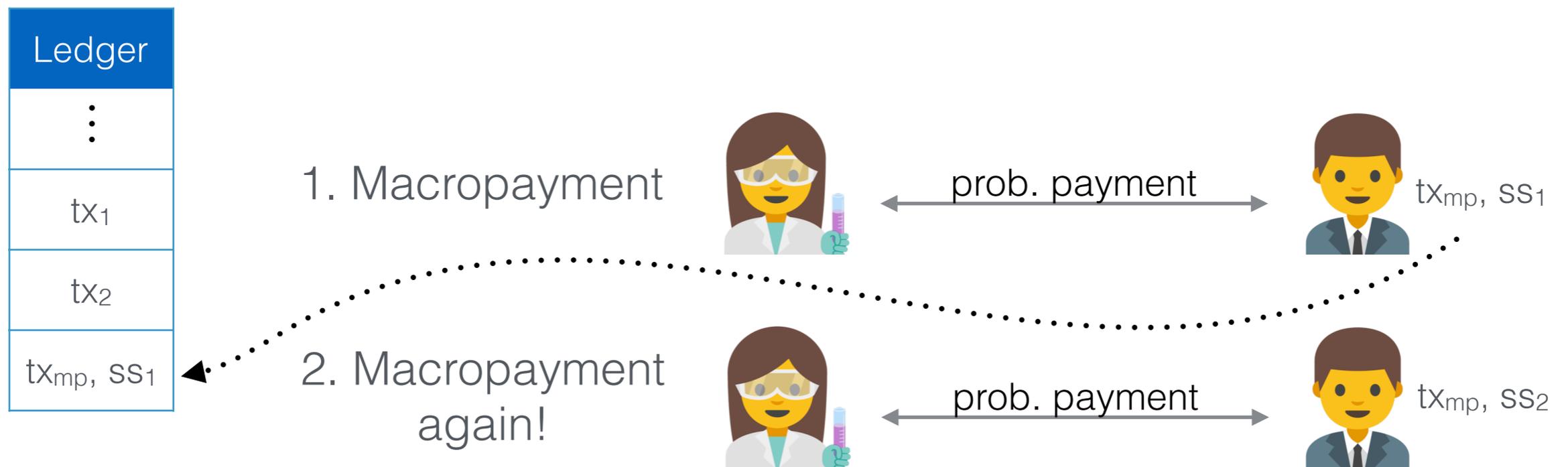
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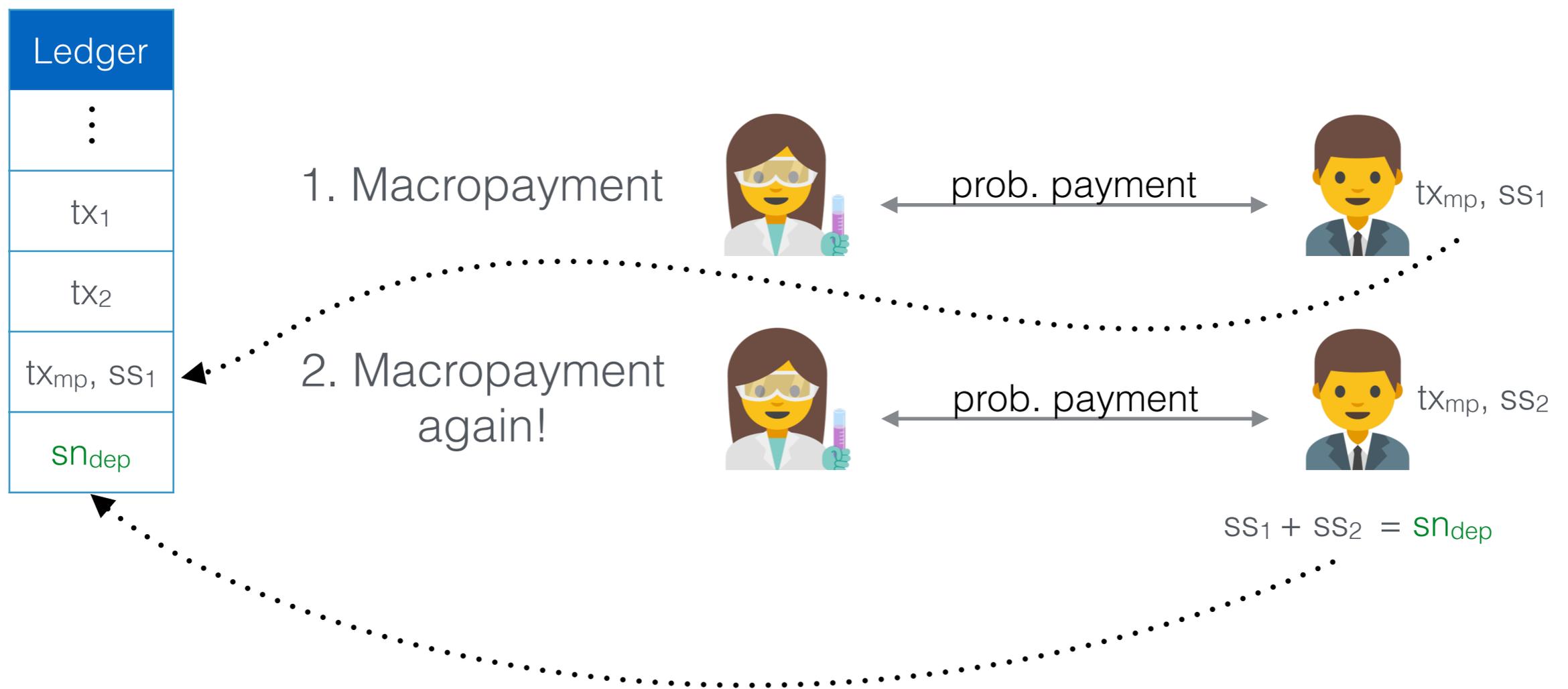
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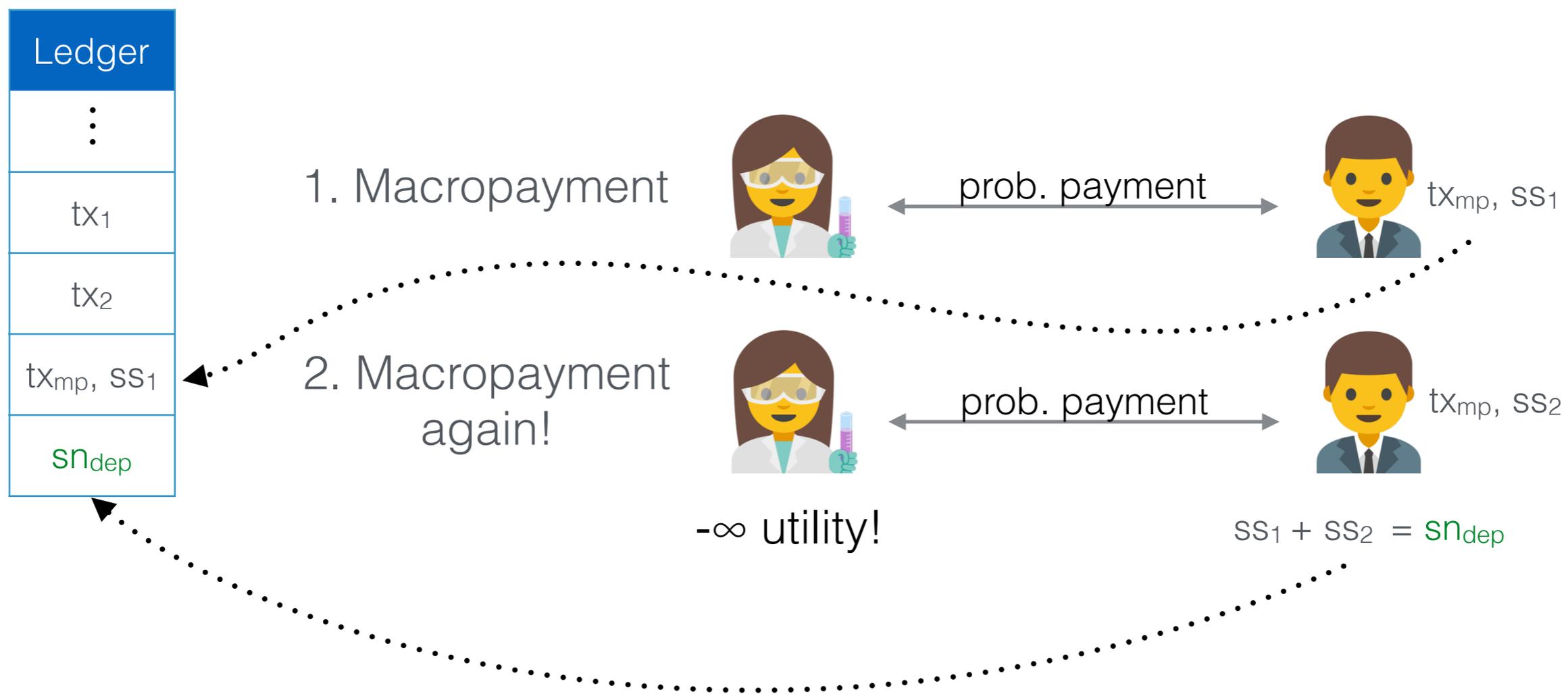
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So far

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Deposits:

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*Feature:* Customers should be able to withdraw deposits.

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See paper for solutions!

# Takeaways

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Thanks!

<http://eprint.iacr.org/2016/1033>